

AN ABSTRACT OF THE THESIS OF

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A testable, biphasic model for protein folding is formulated. In this model, linearly short and medium range interactions dominate early folding, causing the chain to assume independently nucleated modules of persisting structure termed LINC's. In a later stage of folding, the LINC's fold relative to each other, and it is only at this time that the protein assumes its characteristic interior and exterior and its overall globular structure.

In the perspective of the model, a computational approach is outlined, requiring first a systematic examination of steric and energetic constraints that can be calculated with some confidence by accepted means. To this end, calculations were conducted to determine the sterically allowed conformation for:

- 1) a post-helical residue situated at the carboxy-terminal end of a backbone-only helix,
- 2) various side-chains of an intra-helical residue, and
- 3) the constraints imposed on lysyl and arginyl side-chains if some accounting is made for hydration of the respective cationic side-chain moieties.

It is found that substantial steric constraints are engendered in all three cases.

In a second part of this thesis, the secondary structure of nucleic acids is examined. The secondary structure of ribonucleic acids and the genes from which they are transcribed is likely to be a parameter in any recognition and control processes involving these molecules. It is theoretically possible to enumerate the set of all messages, M , consistent with the observed amino acid sequence of a given protein. In practice, this set is computationally too large, being on the order of Avogadro's number for even a small protein. A method is developed to select two distinguished members of M without explicit enumeration. These members are:

\bar{m} - the potential message with maximal secondary structure, and \underline{m} - the potential message with minimal secondary structure.

The distinguished members, \bar{m} and \underline{m} , are extrema that bracket M . They are used to examine the properties of M relative to the degree of secondary structure forced upon the actual biological message and upon the structural gene from which it is transcribed. Although this study leads to some general conclusions about nucleic acid structure, the range between \bar{m} and \underline{m} is too large to permit specific predictions except in a few singular cases where further information is already available. With the exception of these cases, it appears likely that the quest for structural determination will be confined to the laboratory until a larger library of nucleic acid sequence data can be accumulated.

Calculations Relating to the Structure
of Biopolymers

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Any work of mine will always bear the imprint of my teacher, Harry Goheen, who has long fostered the application of automata theory as a paradigm of cognition.

This thesis is dedicated to Harry and Molly Goheen.

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CALCULATIONS RELATING TO THE STRUCTURE OF BIOPOLYMERS

1. Introduction

This thesis divides naturally into two distinct parts, each relating to the structure of informational biopolymers. The first part is concerned with the conformation problem for globular proteins, that is, with the relationship between a protein's amino acid sequence and its three dimensional configuration. The second part is concerned with the secondary structure characteristics of messenger ribonucleic acids and the structural genes from which they are transcribed.

In both parts, proteins and nucleic acids, a canonical set of molecular structures is already inherent in the definition of the problem, and, in each case, the set in question is too large to be computationally useful. For example, it would be helpful to compute the free energy of all reasonable configurations of a small protein and display the result in some representation of protein conformation space. The astronomical number of members in the canonical set precludes such an approach by exhaustion, not only for the example, but for any interesting computation one cares to make.

In both cases, proteins and nucleic acids, it is presumed that the large canonical sets each have a single member (or perhaps a small equivalence class of members) that is the biologically active

representative of that set. In the case of proteins, this member would be the native form of the protein molecule; in the case of messenger-RNA, it would be the actual biological message. In any case, it is this distinguished member that is being sought.

In lieu of a method that permits exhaustive inspection, alternative approaches must be invented. For the conformation problem, the alternative depends upon a new, testable model for protein folding which is presented at the beginning of the next chapter. Using the model, the conformation problem can be partitioned into the summation of several separable, smaller problems, each of which is computationally feasible. In effect, the model provides additional information that can be used to eliminate uninteresting subsets of the canonical set.

No model springs readily to mind for the messenger-RNA problem, and a different approach was taken, requiring the selection of boundary elements from the canonical set. These elements bracket the remaining members of the set, and they can be discovered without explicit enumeration. The selection and application of boundary elements, called characteristic extrema, is discussed in chapter three.

During the course of this work, many computer programs were defined and written. Some of these, such as the computer graphics routines, were of enough general interest to be included in the O.S.U. Computer Center library and will not be further discussed here. There remained, however, a large number of programs whose

interest is particular to this work. This latter category can, in turn, be further divided into three libraries, known as:

- a) PROTEINS - a library of programs used to manipulate protein sequence data and coordinates, and to compute and display molecular energies.
- b) RNA - a library of programs used to manipulate nucleic acid sequence data, and to compute and display selected configurations satisfying the Tinoco stability criteria.
- c) PLIB - a subroutine library containing support routines used in conjunction with other programs.

A synopsis of the major programs in all three libraries is given in the appendix.

II. Tertiary Structure of Globular Proteins

The transition of a denatured protein into its native structure is defined to be a global folding process, whereas any linearly piecewise folding that occurs in a nascent chain is a local folding process. Convincing instances of local folding have been demonstrated in various contexts (1,2). In general, the folded end product is expected to be process dependent because conformational states adopted by partial chains will be deprived of any information that accrues with additional chain growth. That is, a nascent chain cannot foresee its future.

Cases are known, however, in which both local and global folding processes yield the same final structure (3,4). One conception of how qualitatively differing initial states converge to the same final structure rests on the assumption that this structure is necessarily synonymous with a global free energy minimum for the molecule (3). Another conception will also rationalize the directed emergence of a unique conformation from differing initial states. In particular, a biphasic model for folding is proposed here. In this model, linearly short and medium range interactions dominate early folding from any state, and order the polypeptide chain into independently nucleated, persistent modular units of structure. Following this early assembly, linearly long-range interactions are then responsible for the further ordering of modular entities into the full

three-dimensional configuration of the protein.

The general notion of a biphasic model is no longer novel inasmuch as elements thereof are to be found, either explicitly or implicitly, in several recent publications (5,6), and the concept of nucleation events proposed by Levinthal is, of course, well known (7). The attempt here, however, has been to provide a highly specific model that both takes into account the body of experimental evidence and includes sufficient detail to allow a quantitative examination of its consequences.

In detail, it is proposed that the polypeptide chain, dominated by linearly short and medium range interactions, folds initially into Local Independently Nucleated Continuous segments (LINC_s). The ordering of the chain into LINC_s is promoted during any local folding that takes place in a nascent chain, and LINC formation is also favored in a global folding process because the chain will fold into LINC_s before it can fold into anything else.

LINC_s are structurally persistent, separable, modular entities that are precursors to their counterparts in a folded protein. LINC_s are usually, if not invariably, bounded by peptide chain turns (8,9) which are construed to be the conformationally permissive (10) hinges that allow an ensemble of LINC_s to fold relative to each other.

In this model, a protein is comprised entirely of LINC_s and interspersed hinges. Not until the occurrence of inter-LINC_s folding does the protein take on its characteristic interior and exterior

or its overall globular structure. It is at this latter stage in the folding pathway that linearly long-range forces come into play and the LINC's are disposed into their native conformation.

The LINC's and hinges model is consistent with the observation that both local and global processes can yield the same final configuration. The model is also consistent with the success of recent empirical efforts (11) to predict secondary structure based only upon correlations between local amino acid sequences. In the present model, alpha helices and anti-parallel beta pleated sheet are considered as particular instances of LINC's.

Viewed from a perspective prompted by this model, the problem of structure formation can be divided into two parts: prediction of LINC's conformation and prediction of inter-LINC's conformation. Some of the factors limiting inter-LINC's folding in the case of myoglobin suggest that packing constraints and hydrophobic interactions place major restrictions on any possible solution set (12,13).

Turning now to the question of LINC's conformation, a study by Gelin and Karplus (14) finds side-chain torsional angles in pancreatic trypsin inhibitor at or near their expected minima in the free amino acid. Such a result is consistent with the present model, for, within a LINC, short and medium range interactions direct the folding process for side-chains as well. Thus, when an independently nucleated oligopeptide 'jiggles' into a persisting conformational minimum, the side-chains are expected to

populate their respective minima too, because the steric constraints at this stage in the folding process are not comparable to those imposed on a side-chain at the interior of a protein. It might be thought that when the LINC's subsequently fold relative to each other, displacement of the side-chain from a rotational minimum may find compensation in better inter-LINC's packing. In practice, this trade-off becomes less feasible because a side-chain displacement is no longer free to occur independently, but only in cooperation with other structural determinants in the LINC.

In the general case, the problem of predicting the conformation of only a single LINC by complete energy minimization (15) is still too complex to solve directly. In a recent attempt to reduce the computational complexity, each amino acid residue in the protein is represented by just two points (16). While this approximation is presented as being highly successful, it is difficult to believe that the information loss arising from a point representation of the side-chain can yet be consistent with predictive results.

The approach adopted here is to compile a catalog of constraints limiting the conformational freedom of a LINC. The catalog can then be used to winnow conformation space to a limited set of energetically favorable conformations for a given LINC. In this manner, the computational complexity will be suitably reduced without concomitant loss of information.

The remainder of this paper describes computations that reflect the stringent limitations inherent in LINC's packing, based

primarily on steric restrictions.

2.1 Limitations affecting a post-helical residue

Upon termination of a right-handed alpha helix at its C-terminus, the first residue no longer in a helical orientation will be termed a post-helical residue. The subspace of conformation space that can be occupied by selected post-helical residues is now explored.

Figure 1 is a Ramachandran (ϕ, ψ) plot with peptide coordinates taken from Marsh and Donohue (17). This (360 x 360) space was sampled every ten degrees and each 'x' marks a sample point where the dipeptide gly-ala is found to be sterically allowed. The contact distance criteria used to compute steric inhibition were taken from Ramachandran and Sasisekharan (18). Superimposed upon the 'hard-sphere' contact map in Figure 1 are energy contours of a 'soft-sphere' function (19). The good agreement between hard sphere and soft sphere functions is no longer surprising to us, as repulsive forces are known to play a dominant role in such functions. To facilitate discussion, dipeptide space is partitioned and named as shown in Figure 1.

Inspection of Figure 1 shows a narrow energy well in the map area corresponding to right-handed alpha helix. For helical residues populating this region of the map, narrowing of the well ought to be further enhanced by hydrogen bonding within the helix.

Allowed positions for the dipeptide gly-ala. Positions found to be sterically allowed are indicated by an X. Some favorable energy contours are outlined, and the regions are named.

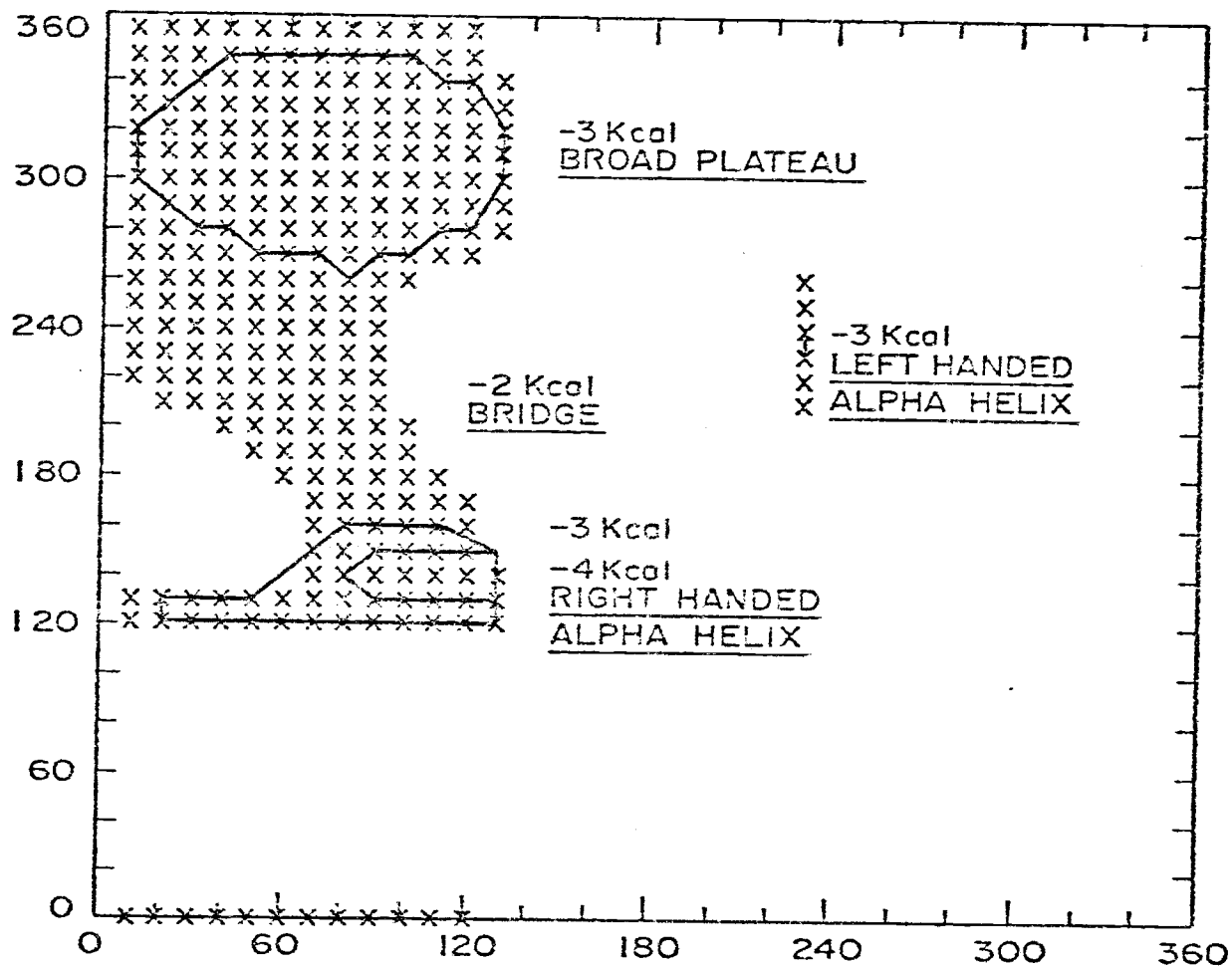


Figure 1

This expectation appears to be borne out for the refined x-ray structure of lysozyme (15,20) by the apparent clustering of (ϕ, ψ) values in the neighborhood of $\phi = 120$, $\psi = 130$. This is the only high density cluster of points in the (ϕ, ψ) plot of lysozyme.

I first examine steric constraints resulting from backbone-only interactions between a post-helical residue at the carboxyl end of a right-handed alpha-helix and the four preceding residues; all five residues are backbone-only residues. A backbone-only residue is one without a side-chain; it can be viewed as a des-methyl L-alanyl residue. Steric constraints imposed on a backbone-only residue are the minimal constraints for any actual residue, regardless of the nature of the side-chain.

With one turn of backbone-only helix preceding a backbone-only post-helical residue, only the conformations shown in Figure 2(a) are allowed. This restriction of conformation space is due to steric interference between the backbone atoms in the post-helical residue and the adjacent carbonyl oxygen from the preceding turn of the helix. Since the restriction involves only backbone atoms, every post-helical residue is at least this restricted.

When the side-chain in a post-helical residue is also taken into consideration, further structural limitations are seen. While a post-helical backbone-only residue is not distinguishable in this analysis from a post-helical alanine, differences do begin to appear with further increases in side-chain size. Corresponding diagrams for the cases of histidine and tryptophan are shown in Figure 2(b)

Sterically allowed positions for the first post-helical residue adjoining the C-terminus of a backbone-only α -helix.

- (a) Allowed positions for a backbone-only residue. Backbone-only residues are allowed only in the area shaded by diagonal lines.
- (b) Allowed positions for Trp and His.
- (c) Allowed positions for Trp only.

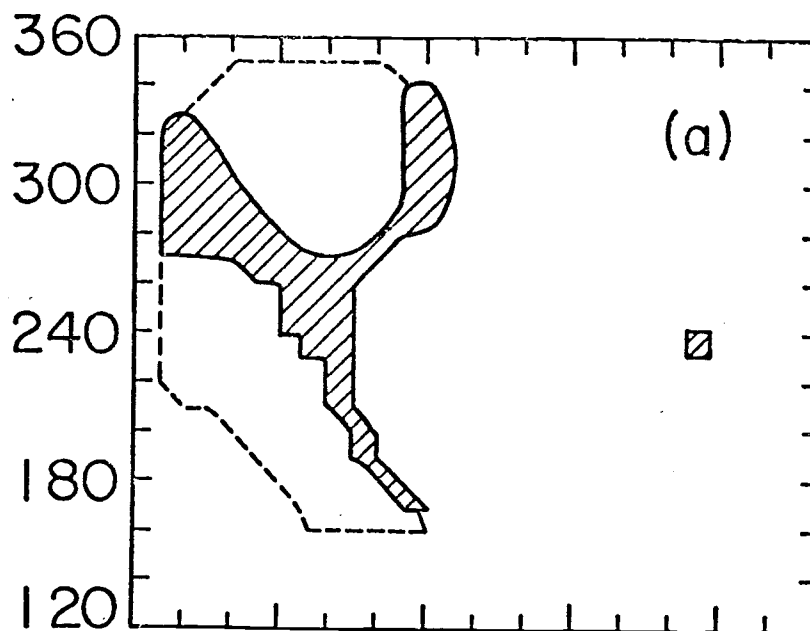
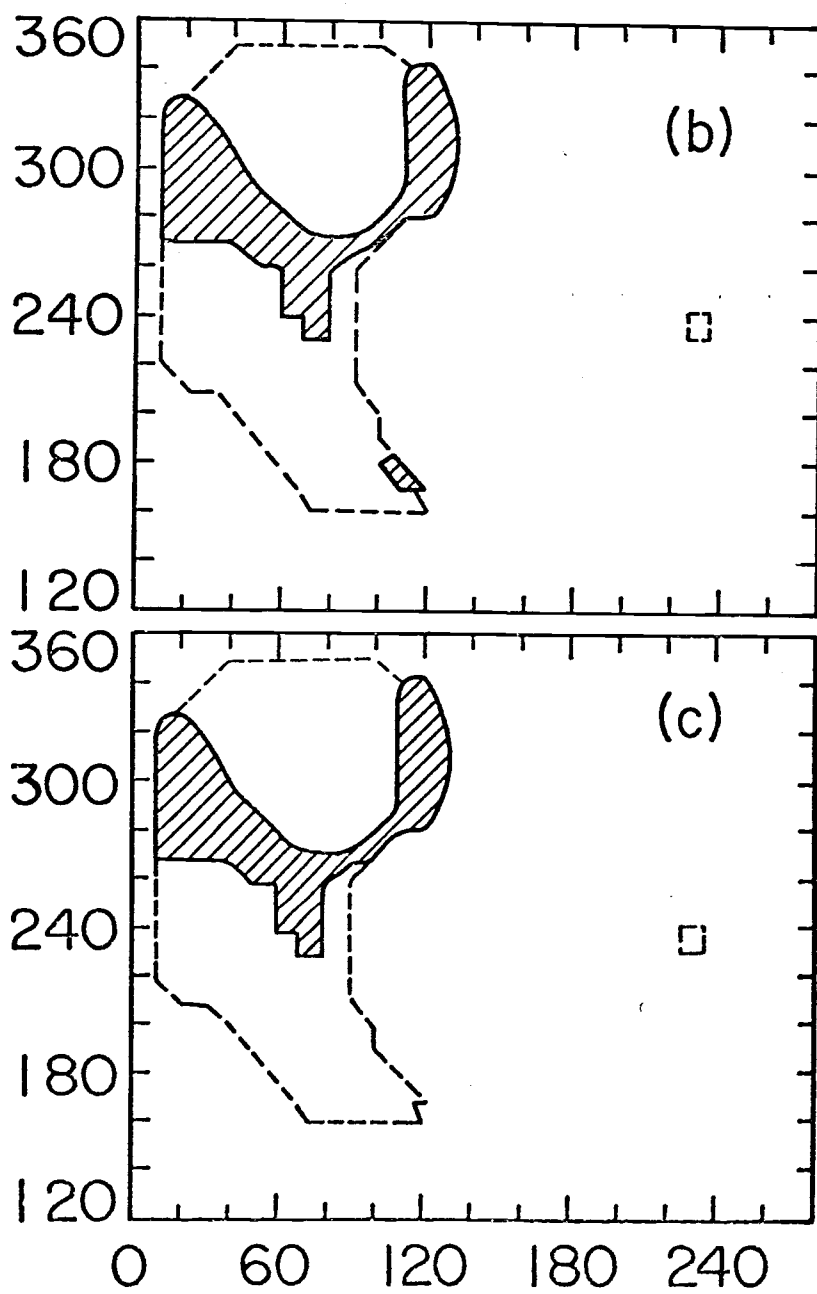


Figure 2

Figure 2 (Continued)



and Figure 2(c). In this computation, side-chain configurations arising from the domain $\chi^1 = 60^\circ, 180^\circ, 300^\circ (\pm 10^\circ)$ and $\chi^2 = 0^\circ, 90^\circ, 180^\circ, 270^\circ$, were examined. It can be seen from the figure that the side-chains can impose significant additional constraints on the possible disposition of a post-helical residue.

The structural limitations shown for post-helical residues are based on the assumption of energetically well-formed helix (21). When the helix used for these computations is appropriately distorted at a constraining locus, there is an accompanying relaxation of the observed constraints.

In addition, deviation from the ideal peptide geometry used here may tend to reduce the limitations shown in Figure 2. However, an attempt has been made to compensate for this possibility by a conservative choice of contact distance criteria. Studies on steric hindrance show a sensitive dependence upon the choice of contact distance criteria (17), with the Ramachandran values being the most conservative set proposed.

2.2 Limitations affecting an intra-helical residue

A second example of stringent packing constraints is seen in the case of an intra-helical residue. The helix-breaking tendency of proline due to steric effects was observed some time ago (18,22). In this second example, attention is focused on the converse steric effect, limitation of side-chain freedom by the helical backbone.

Each of the amino acids listed in Table 1 was included as the middle residue between two turns of backbone helix (i.e. $(\text{gly})_4\text{-X-(gly)}_4$ where X is the residue under inspection). The side-chains were then examined at configurations where side-chain groups are in one of the conventionally observed torsional minima. Aliphatic groups were varied over the domain 60° , 180° , and 300° ($\pm 10^\circ$), while planar and aromatic groups were varied over the domain 0° , 90° , 180° , and 270° . Table 1 summarizes the positions found to be sterically allowed. Backbone helix is seen to strongly limit the accessible side-chain structures of several amino acid residues.

In the formation of a LINC, charged polar residues are probably hydrated. The attachment of a hydration shell to the terminal group of arginine or lysine, for example, will increase the packing constraints. To approximate hydration effects, x-ray data from salts of arginine and lysine (23, 24, 25) were examined and water molecules were attached to the terminal groups at loci where hydrogen bonding was observed in the crystal structures. The water was oriented so that its hydrogen atoms were symmetrically positioned above and below the plane of the side-chain group. The hydrated amino acid residues, $\text{Lys}\cdot(\text{H}_2\text{O})_3$ and $\text{Arg}\cdot(\text{H}_2\text{O})_5$ were then used in the intra-helical computation. In Table 1, it can be seen that the inclusion of hydration tends to force both arginyl and lysyl side-chains towards extended chain configurations.

Table 1

(Gly)₄-X-(Gly)₄ in Helix

Domain A	position	I = $60^{\circ} \pm 10^{\circ}$ II = $180^{\circ} \pm 10^{\circ}$ III = $-60^{\circ} \pm 10^{\circ}$
Domain B	position	I = 0° II = 90° III = 180° IV = -90°

The domains given for each residue are the domains of definition over which each side-chain group was varied, listed in sequential order of increasing distance from the C-alpha along the side-chain. For example, Tyr has two degrees of rotational freedom in its side-chain arising at the C^α-C^β bond and at the C^β-C^γ bond. With two degrees of freedom, it is necessary to specify two domains of definition. These are listed in the table below as A,B where domain A pertains to the C^α-C^β bond and domain B pertains to the C^β-C^γ bond.

<u>Residue</u>	<u>Domain</u>	<u>Allowed Positions</u>	<u>Hydrated Form Allowed Positions</u>
LYS	A, A, A, A	II, II, II, I-III II, I, II, I-III III, II, II, I-III III, III, II, I-III	II, II, II, II II, I, II, II III, II, II, II III, III, II, II
CYS	A	II III	
GLU	A, A, B	II, I, II or IV II, II, II or IV I, II, II or IV I, I, II or IV	
HIS	A, B	II, II or IV	
MET	A, A, A	II, I, I or II II, II, I-III III, II, I or II III, III, II or III	
ASP	A, B	II, II or IV	

Table 1 (continued)

<u>Residue</u>	<u>Domain</u>	<u>Allowed Positions</u>	<u>Hydrated Form Allowed Positions</u>
THR	A	III	
TYR	A, B	II, II or IV	
SER	A	II III	
VAL	A	III, III	
ILU	A, A	III, II or III	
LEU	A, A	II, II III, III	
PHE	A, B	II, II or IV	
TRP	A, B	II, II or IV	
ARG	A, A, A, B	II, II, II or III, I or II or IV II, II, I, I or IV II, I, II, I or II or IV II, I, I, I or IV III, II, II, I or II III, II, I, I or IV III, III, II, I or or II or IV III, III, III, I or II	II, II, II or III, I or II II, I, II, I II, I, I, I or IV III, II, II, I III, II, I, I or IV III, III, II, I III, III, III, I or II

Table 2

(Gly)₄-LYS-ARG-(Gly)₄ in Helix

Domains are defined as in Table 1. Any of the allowed positions listed for lysine are sterically compatible with any of the allowed positions listed for arginine. All other pairwise positional arrangements are sterically incompatible.

Allowed Positions
for Hydrated Lysine

II, II, II, II
 II, I, II, II
 III, III, II, II

Allowed Positions
for Hydrated Arginine

II, II, II, I
 II, II, III, I or II
 II, I, II, I
 II, I, I, I or IV
 III, III, II, I
 III, III, III, I or II

2.3 Limitations affecting adjacent intra-helical lysyl and arginyl residues

As a final experiment, sequentially adjacent lysyl and arginyl residues, both intra-helical, were inspected to see whether such a juxtaposition imposes constraints in addition to those experienced by these residues taken individually. Additional constraints were observed, as summarized in Table 2.

2.4 Summary and conclusions

The values obtained from the preceding computations were not compared to values available from x-ray studies since a correspondence between individual torsion angles will depend in part on factors not included here. These initial computations have employed an idealized moiety called backbone-only helix, and with it, the assumption of a completely regular geometry for a helix. While helical fibers of poly-L-alanine appear to be compatible with these assumptions (26), it is not expected that a heterogeneous collection of helical residues will exhibit equivalent regularity. For these reasons, it is felt an appropriate test of the model must wait until predicted LINC's can be compared to their x-ray elucidated counterparts in solved structures.

In closing this section, it should be noted that the LINC's and hinges model is the simplest representative taken from a spectrum of related models. In the preceding paragraphs, emphasis

has been placed on the similarity in structural identity of a LINC from the onset of structure formation through folding to incorporation in the final globular assembly. The model is simple in a computational sense, because, with these assumptions, the approximate structure of a given LINC can be calculated without regard for its neighbors and then treated as a single structural entity during subsequent computations. It is possible, however, that when the ensemble of LINC's is packed into a final globular assembly, a more extreme deformation of the original structures occurs. In the most extreme case, the original structure would be deformed beyond recognition, but for reasons given earlier, this extreme is thought to be unlikely. In the event that limited deformation takes place during inter-LINC's assembly, the initial conformation of the undeformed LINC would serve as a suitable starting structure.

In summary, a testable biphasic model for the folding of globular proteins has been proposed. In this model, linearly short and medium range interactions dominate early folding, causing the chain to assume independently nucleated, structurally persistent modular units of structure; these postulated entities are termed LINC's. In a later stage of folding, the LINC's fold relative to each other, forming a structure in which linearly long-range interactions also play a role. It is only at this time that the protein assumes its characteristic interior and exterior and its overall globular structure.

If these ideas about the folding process are valid, then demonstrable stabilizing forces must exist in oligopeptides of

even moderate size. One strong source of structural stabilization is steric repulsion, and, to this end, some packing constraints for intra-helical and post-helical residues have been shown. Additional work will be necessary to further develop the catalog of structural determinants for a LINC. At the same time, an exploration of the interfaces between LINC and hinges will be required. In the transition from a LINC to a hinge, steric constraints can no longer take such a key role, since by these working assumptions hinges are comparatively flexible. In order to predict the locations of these interfaces, it will be necessary to have some further accounting of hydrogen-bonding and hydrophobic interactions.

III. Secondary Structure of Ribonucleic Acids

The secondary structure of ribonucleic acids and the genes from which they are transcribed is likely to be a parameter in any recognition and control processes involving these molecules. For example, the half-life of mRNA varies widely in eukaryots, ranging from a few seconds to many hours (27). The notion that the secondary structure of RNA correlates with such half-life differences is consistent with the observation that rRNA and tRNA have both a high degree of secondary structure and a comparatively long half-life (28). The explanation for increased longevity as a function of increased secondary structure is probably related to the action of ribonuclease which will preferentially degrade single stranded RNA over double stranded RNA (29).

Evolutionary considerations are also of concern here. If there exists a structure:function correlation in ribonucleic acids, then particular configurations should enable or enhance biological function, and we may therefore expect selection pressures to play a role in the evolution of these molecules. Since there is no a priori reason to believe a mutation that confers benefit on the message will also benefit the protein, it is necessary to ask whether conflicts do occur, and, if so, how they are resolved.

Recent attention has been focused upon configurations of 'twofold rotational symmetry' or palindromes in the base

sequences of genes. Such apparently diverse mechanisms as the Lac control region (30), the recognition sites for restriction enzyme action (31), and the DNA renaturation experiments of Wilson and Thomas (32) all implicate palindromic sequences in a seemingly central way. Palindromes fall naturally within the scope of interest of this study since an RNA sequence transcribed from a palindrome will energetically favor a hairpin secondary structure. Indeed, it seems likely that some of the helical regions in RNA are merely structural artifacts that are carried over from the DNA structure. Conversely, at least some palindromes must be forced in order to satisfy functional constraints imposed upon the RNA; the clover leaf structure of tRNA serves as a likely example.

3.1 Messenger RNA

To date a few mRNA's have been isolated, purified, and to some extent characterized. These include the message for silk fibroin, for wheat gluten, for the zymogen of cocoonase, and for a composite of the histones (33,34). While encouraging, this work has not yet been sufficient to prompt general conclusions.

One prospect for anticipating eventual experimental evidence is to make a statistical estimate of RNA secondary structure from a known amino acid sequence. This method may be coupled with deductions from available RNA sequence data. These techniques have been explored by White, Laux, and Dennis (35,36) and by Mark and

Petruska (37). Another approach lies in the possibility of enumerating and characterizing the entire set of messages that could code for a single protein. If fortuitously this set of potential mRNA's all have some interesting property in common, it follows that the actual mRNA would also share this property.

Unfortunately, the set of all messages, M , consistent with the amino acid sequence of even a small protein is computationally unwieldy, to say the least. In the case of ribonuclease, for example, M has 7.5×10^{22} members, almost on the order of Avogadro's number.

Without explicit enumeration, however, it is always possible to choose two distinguished members from the set M . These are:

- 1) \bar{m} - the potential message that exhibits maximal secondary structure, and
- 2) \underline{m} - the potential message that exhibits minimal secondary structure.

The algorithm for selecting \bar{m} and \underline{m} requires either a permissive or a restrictive choice whenever an unspecified base is encountered.

The distinguished elements \bar{m} and \underline{m} are characteristic extrema that bracket the set M . They are, in effect, a least upper bound and a greatest lower bound on the degree of secondary structure of any arbitrarily chosen member of M . As such, \bar{m} and \underline{m} may provide a way to characterize M without resorting to explicit enumeration. For example, if \bar{m} exhibits only a small degree of secondary structure, then it is clear that the actual biological message also has only a small degree of secondary structure. On the other hand, if \underline{m}

exhibits a high degree of secondary structure, then the actual message also has a high degree of secondary structure.

The existence of characteristic extrema for any set M is interesting to the degree that it provides a tool to test interesting hypotheses about the secondary structure of mRNA's. One such hypothesis is that, in the general case, long-lived message confers a selective advantage on a cellular system, for in this case less metabolic energy is required to maintain the message pool in a steady state condition. Such a hypothesis is promoted by the observation of very long-lived message in a situation where the correlative protein is required in great abundance (27). The mechanism of action of ribonuclease further suggests that long-lived mRNA will have a high degree of nuclease resistant secondary structure (29).

Many realistic considerations have been excluded from this hypothesis such as the effect of ribosome attachment on nuclease action or the use of scarce tRNA's as protective masking devices. These simplifications are appropriate as the first object of this exercise is to see what kind of insight the application of characteristic extrema can provide into problems of this type.

A prediction of the hypothesis is that proteins with greater evolutionary latitude will have messages with proportionately higher secondary structure since a mutation that confers a structural advantage on the message may well alter the amino acid sequence of the protein. Hence, arranging a set of proteins in order

of increasing unit evolutionary period should arrange their respective messages in order of decreasing secondary structure.

To test this prediction, a set of sequenced proteins with differing unit evolutionary periods was chosen for examination. These included the histones f2b and f2a1, human cytochrome c, and the alpha and beta chains of hemoglobin (38). In each case, the characteristic extrema were computed and inspected. The degree of secondary structure was measured using a method of Tinoco et al (39). The method consists of forming a matrix with diagonals that reflect all possible hydrogen bonded arrangements that can exist between bases. Thermodynamic criteria are then applied to assess the stability of each arrangement, and unstable loops are identified. While there is a minor disagreement about the thermodynamic criteria used to predict hairpin loops at the lower margin of stability in model systems, it is unlikely that computation of this threshold presents a problem in biological systems. In R17, MS II, and tRNA (38) the biologically significant configurations are more than stable; they are conspicuous.

The Tinoco matrix developed from a protein is going to be quite complex in appearance. If the protein has n amino acids, then the matrix has $(6n-1)$ diagonals. In order to simplify this array, a program was developed to scan each diagonal in turn, remove any unstable structures, and extend stable folding trends to allow easier reading.

Examination of these data showed that the m for all five

proteins could be entirely tied up in hairpin loops, while the \underline{m} in each case was virtually devoid of loop structures. In retrospect, this result is hardly surprising since a loop alignment that avoids a 3:3 registration between the indeterminate third bases would stabilize loops for \mathfrak{m} and destabilize them for \underline{m} . Hence, M is too large, and the range between \mathfrak{m} and \underline{m} is too broad to distinguish between the messages for these five proteins in this fashion. As a corollary to this conclusion, it appears that the set M is sufficiently rich that evolutionary changes in the protein need not occur at the expense of structural constraints on the message.

3.2 Large Palindromes

The set of messages, M , coding for a given protein has been shown to be very large. Nevertheless, it is always possible to single-out two boundary messages that bracket this set with respect to the degree of secondary structure. These distinguished members, \mathfrak{m} and \underline{m} , trap all remaining elements of M between them. In the general case, though, the range between \mathfrak{m} and \underline{m} is too large to permit the existence of an effective forcing function on remaining members of M .

An article by Wilson and Thomas (32) reported the detection of very long palindromes in eukaryotic DNA. These palindromes are said to range from 300 to 6000 nucleotides in length, and experimental evidence indicates they are quite exact, with fewer than one

percent base pairing differences.

If a very long, almost perfect palindrome is transcribed, its transcript should exhibit a hairpin loop of corresponding length. The loop, in turn, will appear as a long trace down a diagonal of the Tinoco matrix on the message. While imperfect pairing may cause a small gap in the trace, or even a jog over to another nearby diagonal where the trace is continued, such irregularities will not be sufficient to obscure the overall pattern in the matrix.

The existence of an extended trace in the Tinoco matrix imposes a severe structural constraint on the message, for in this case the high percentage of overall secondary structure must be packed into a single hairpin loop. For any protein, P, of known sequence, we can develop \mathfrak{m} , the potential message in M that is most permissive of secondary structure, and this extremum can be examined for the existence of a long trace. If that trace is not apparent in \mathfrak{m} , then we may conclude it does not appear in any message in the set M, and it follows that the gene for P does not contain a large palindrome. A representative collection of proteins was examined, and in each case the \mathfrak{m} for the protein was inspected for the existence of a long trace. A trace of suitable length was never found, and the tentative conclusion was reached that long palindromes do not reside in structural genes. Of course, the one configuration that cannot be excluded in an experiment of this sort is the possibility that a structural gene comprises half

or less of an even larger palindrome.

The test set of proteins included the alpha and beta chains of hemoglobin, the histones f2a1 and f2b, and human cytochrome c. From each, an π was computed together with the Tinoco matrix on that π . A computer program was written to pass a window of fixed size down every diagonal, advancing each frame one base pair at a time from upper right to lower left. Frames with complementary base pairing in excess of a specified threshold were marked. The window size and the percentage threshold were parameters to the program.

With a window of 35 base pairs and a pairing threshold in excess of 98%, no subtrace was found in the entire matrix of any protein in the test set. Relaxing these criteria to 85% pairing in a window of 25 base pairs, the trace patterns shown graphically in figure 3 were observed. These criteria are considered highly relaxed in view of the experimental evidence cited. A window size of at least an order of magnitude larger than the one used, as well as a pairing threshold in excess of 99% is indicated in the experimental studies.

The use of highly relaxed detection criteria coupled with the use of π , which is really an upper bound on possible pairing, assure that no palindrome, as characterized by Wilson and Thomas, escaped notice by falling just below the margin of detection.

As a control for the above experiment, the MS2 coat protein cistron was subjected to the same treatment as the π for a protein

Figure 3

The graphs represent the Tinoco matrix of the MS2 coat protein cistron, an illustrative test region from the cistron, and proteins in the test set. Each diagonal was scanned by a program to find continuous regions with more than some specified threshold of pairing. The ratio shown in each figure is the pairing threshold over the window size in base pairs. Diagonal lines mark anti-parallel helical regions where these criteria were satisfied. The vertical scale is graduated in base pairs, while the horizontal scale is a nominal one; both scales divide the message into ten equal regions.

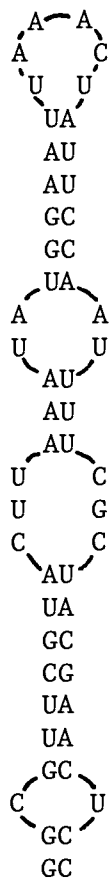
A diagonal line in one of the figures can be translated into the more typical hairpin diagram by using the axes to locate that diagonal within the matrix. The particulars of the pairing pattern can then be discovered by referring to a detailed printout of the Tinoco matrix. For example, the diagonal in the MS2 cistron test region that pairs bases 54,3,2,... with bases 2,3,4,... respectively is diagonal 55. In printout form, that diagonal appears as follows:

Diagonal 55.

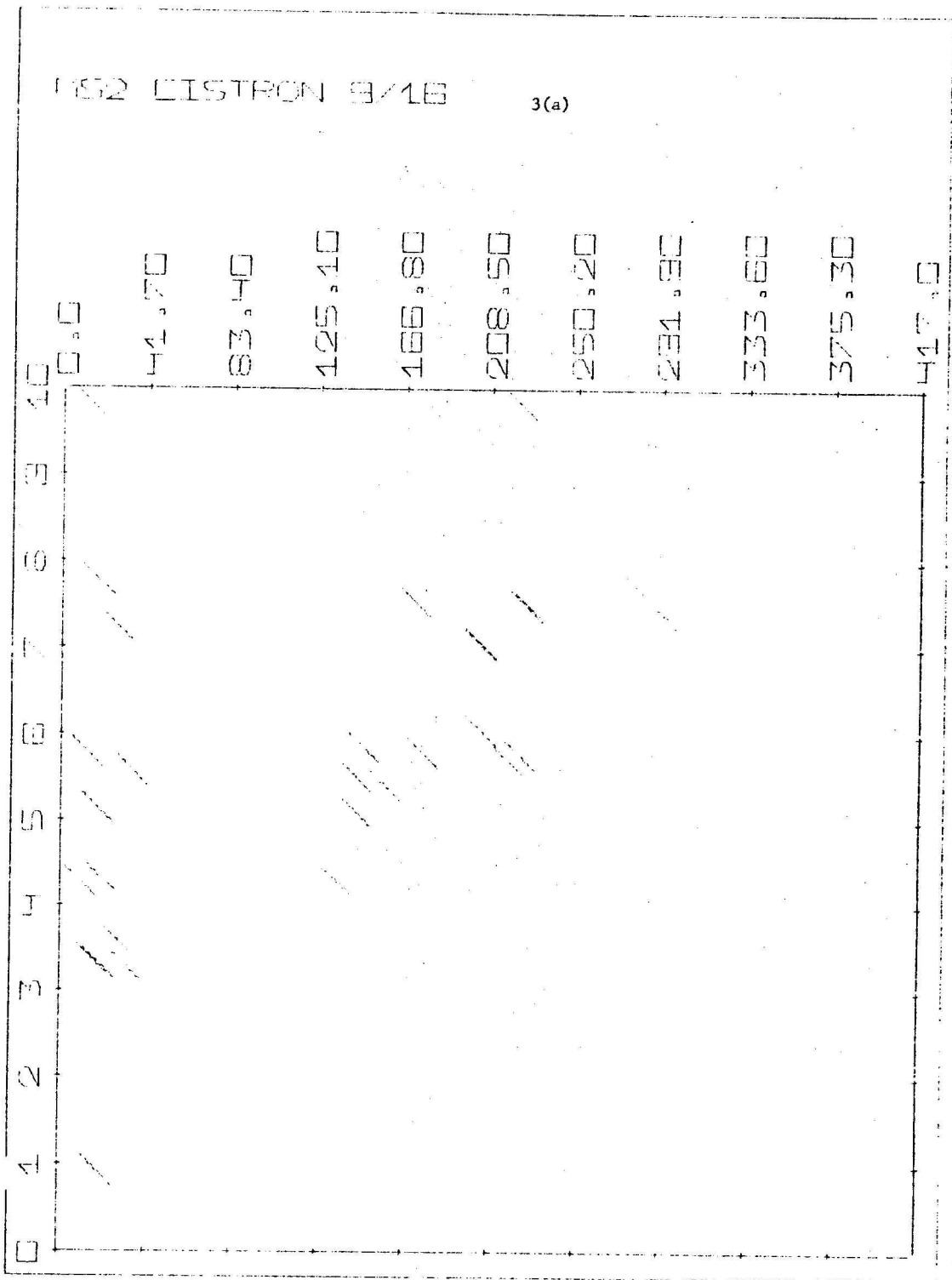
base	5555554444444444333333333322
number	5432109876543210987654321098
base	GCCUCAAGCAUCGCUUUAACCUUAUCA
score	22 2112211 111 122111
base	UGGCGUUCGUACUAAAUAUGGAAUJAA
base	1234567890123456789012345678
number	11111111112222222222

Figure 3(continued)

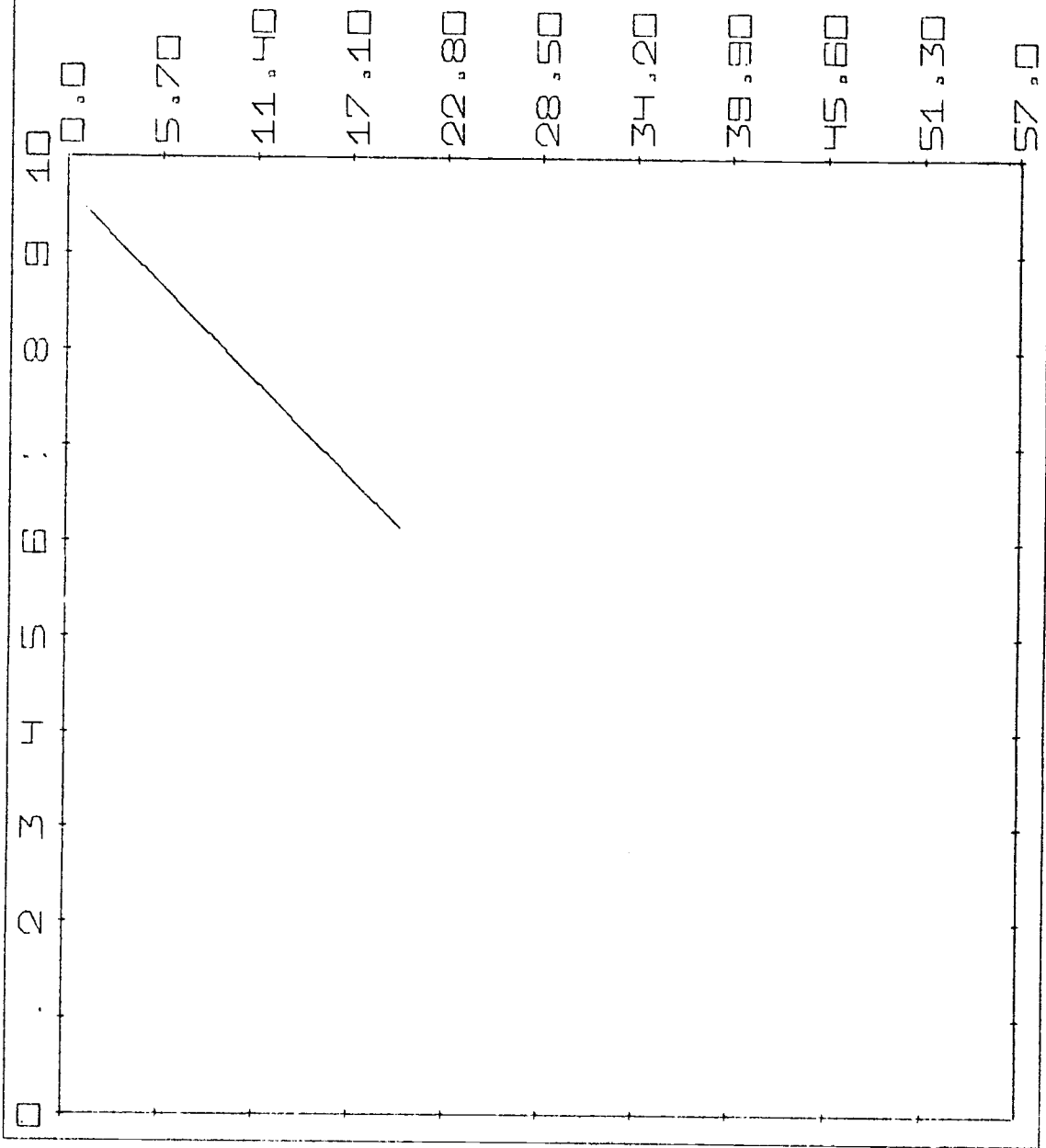
In the more familiar pictorial format, the helical region appears as:



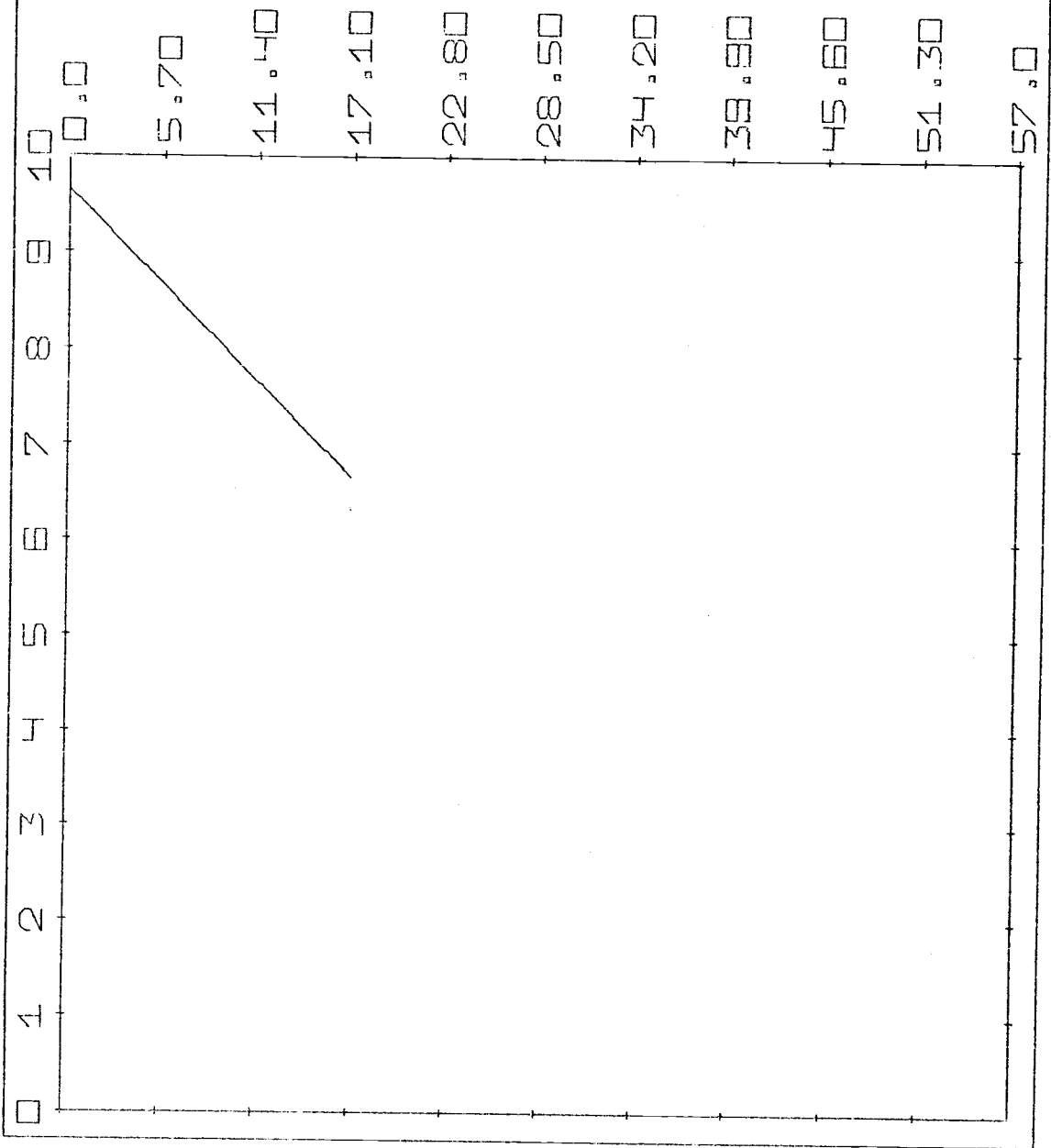
Best scan available.



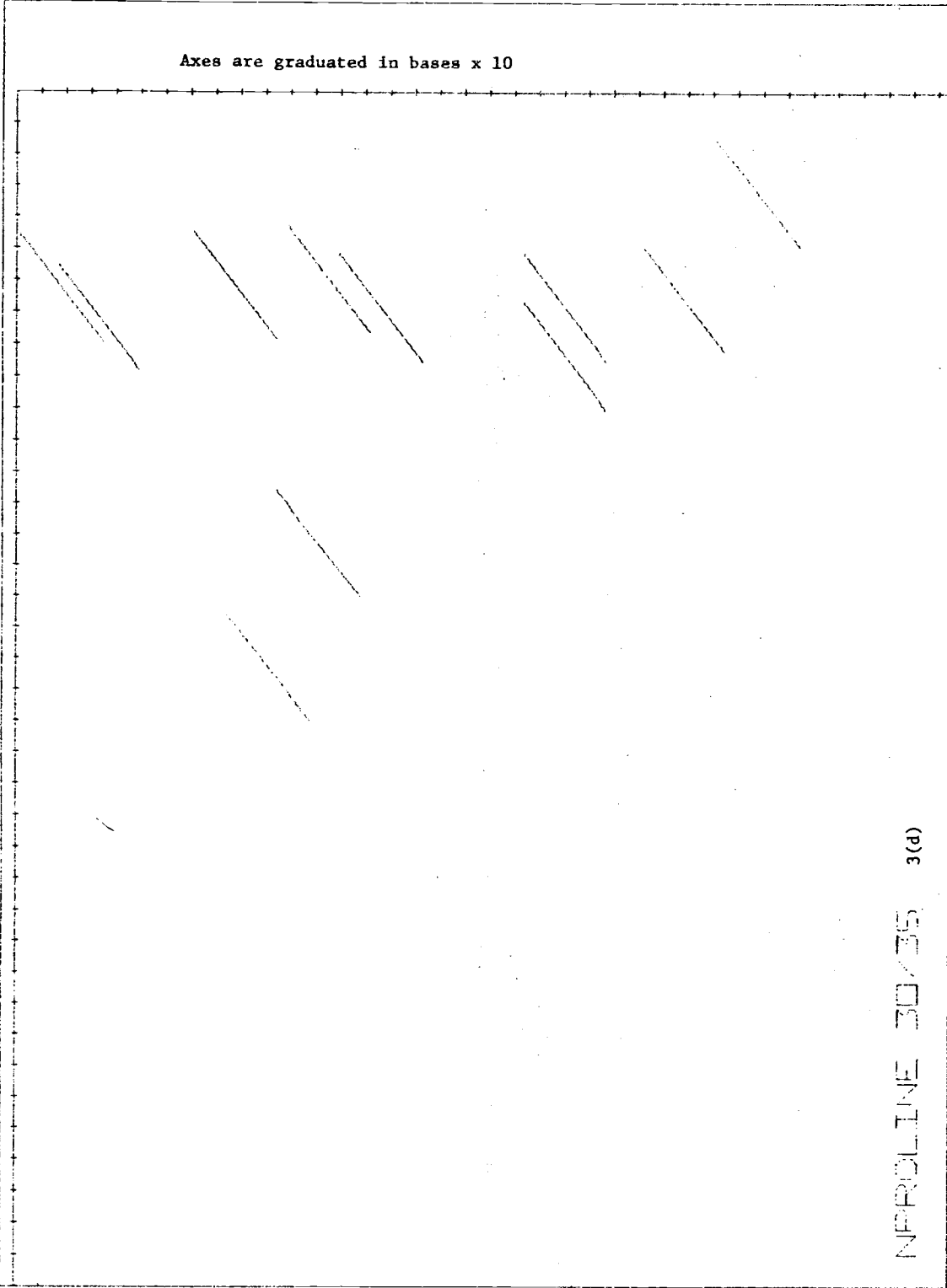
MS2 TEST CISTRON 14/20 3(b)



MS2 TEST CISTRON 12/18 3(c)

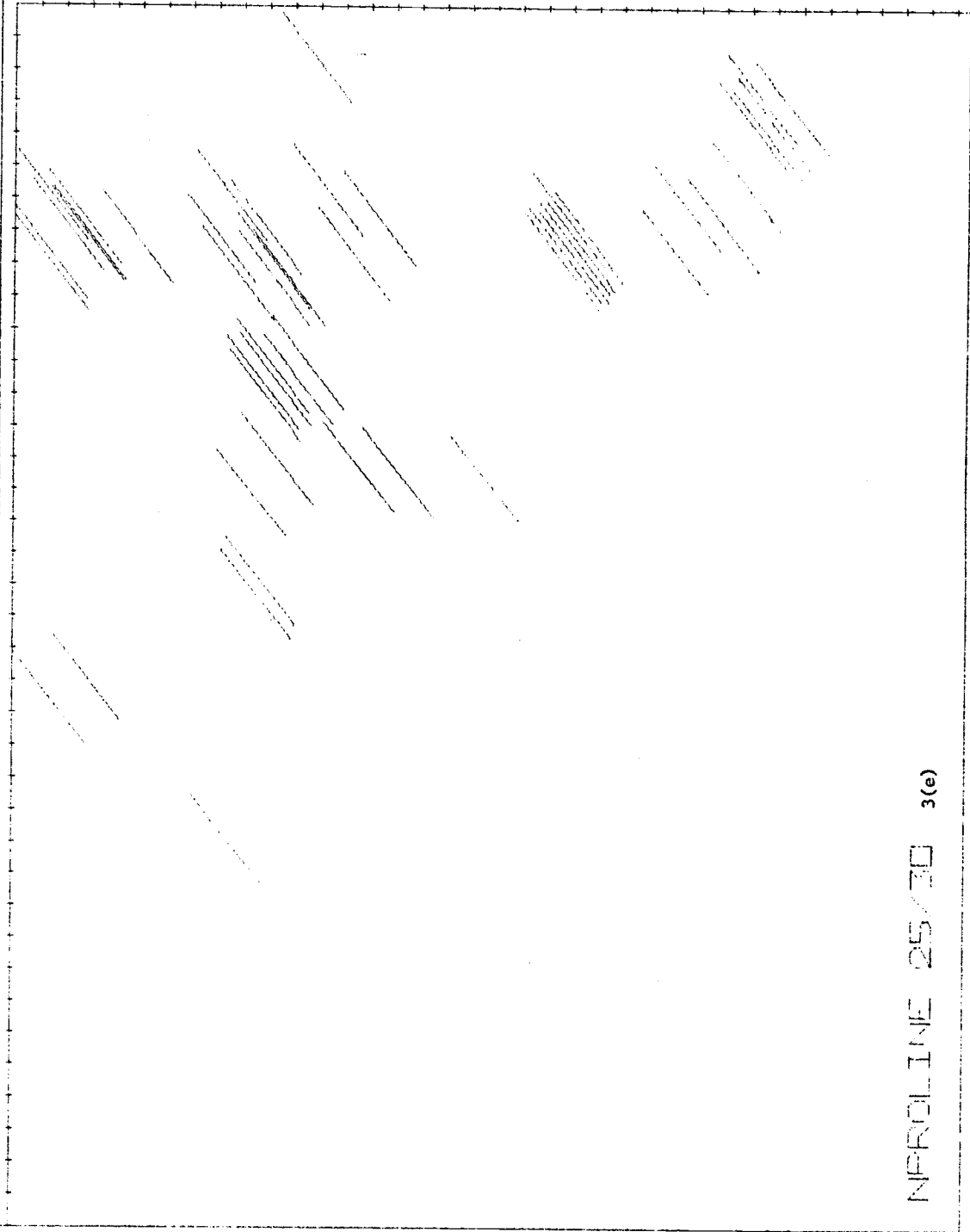


Axes are graduated in bases x 10



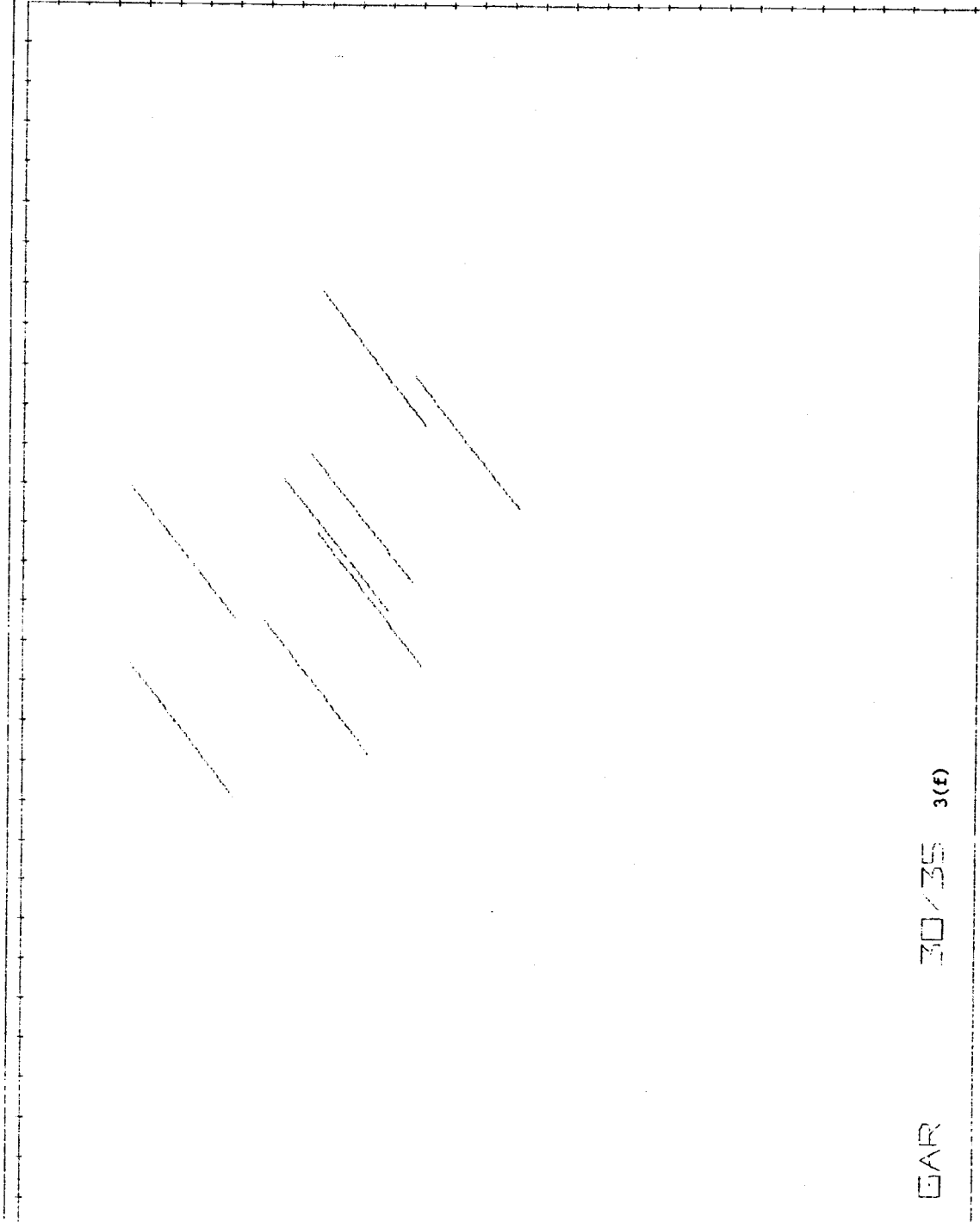
NPRDLINE 30/35 3(d)

Axes are graduated in bases x 10



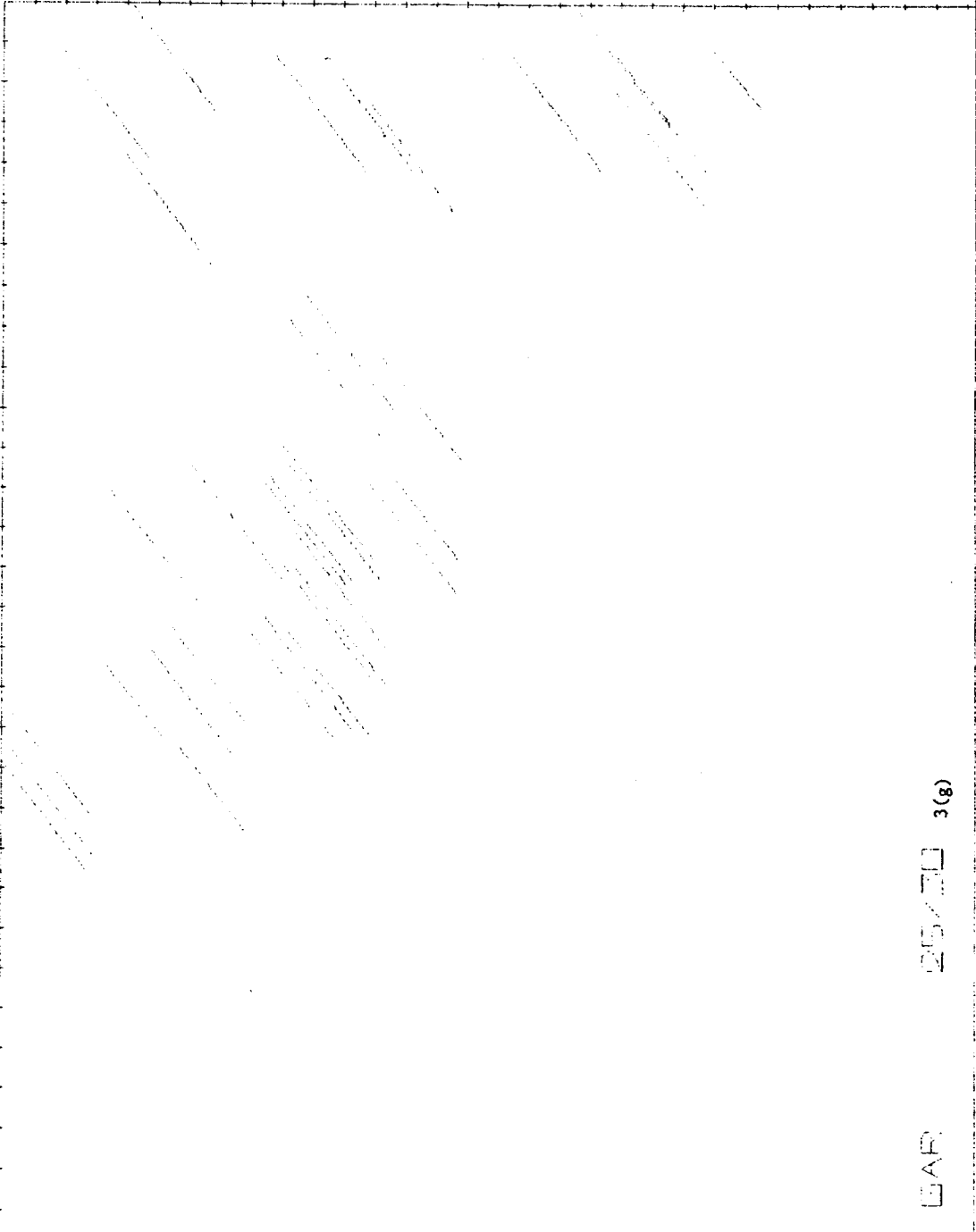
NPROLINE 25/30 3(e)

Axes are graduated in bases x 10



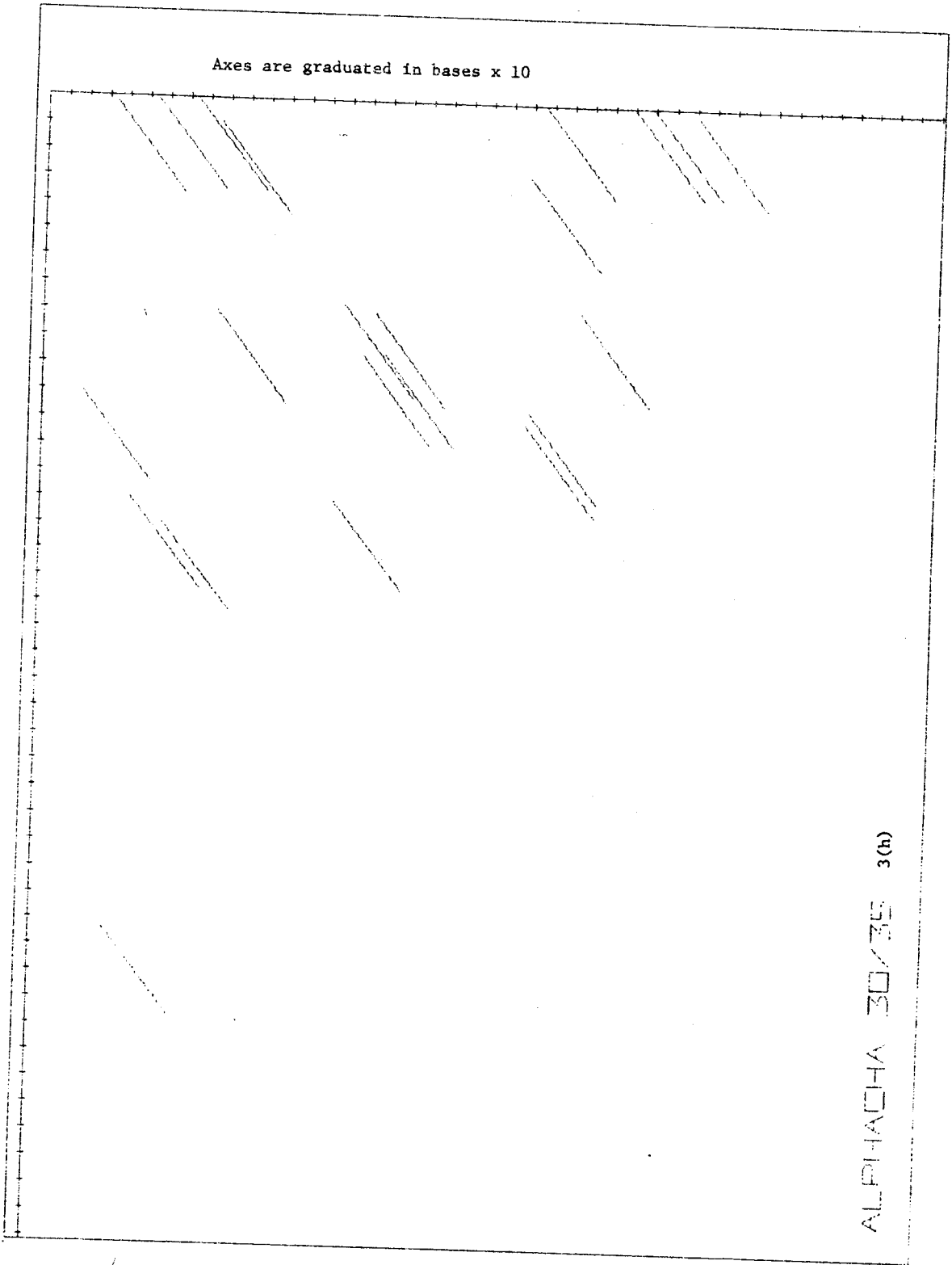
GAR 30/35 3(F)

Axes are graduated in bases x 10



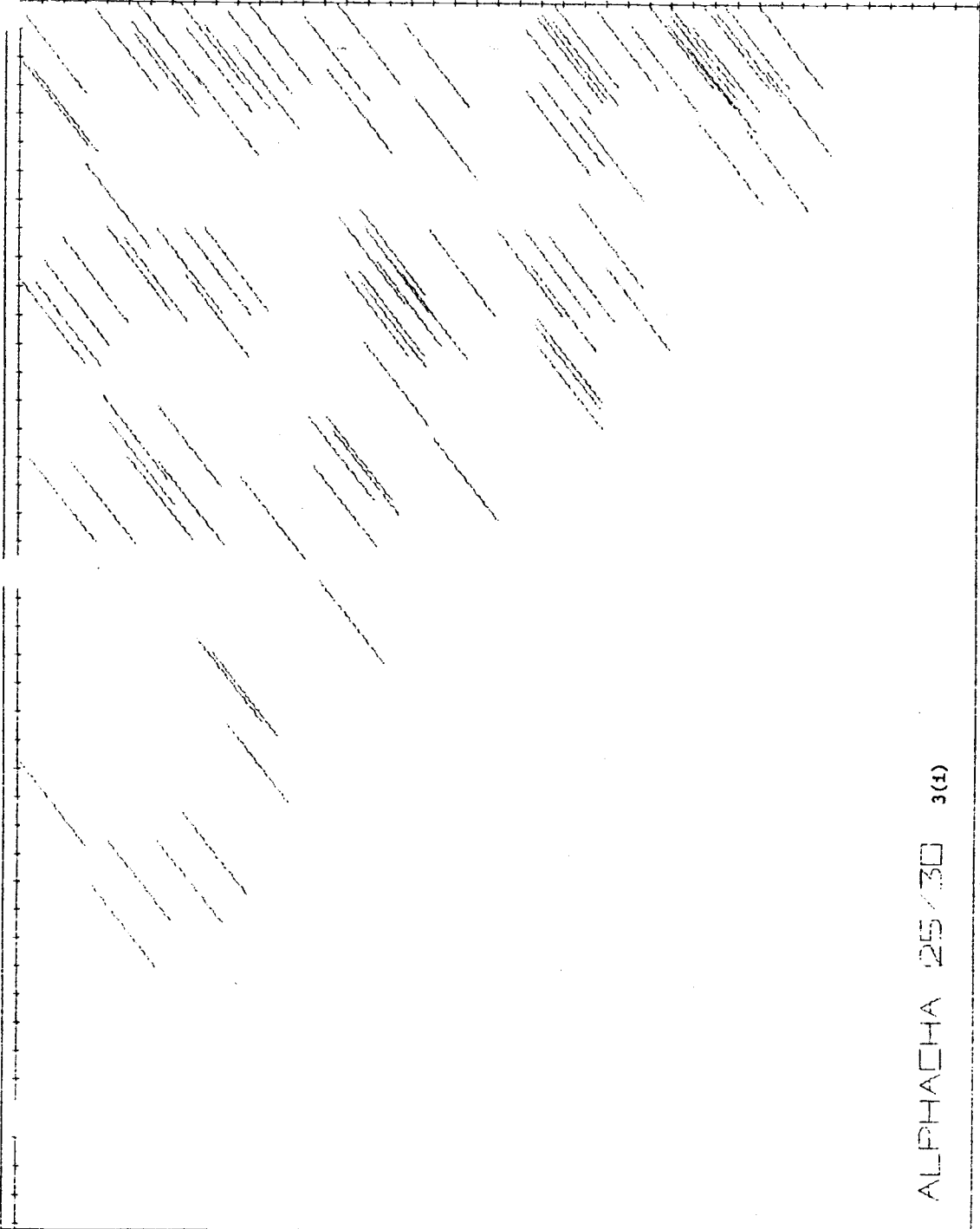
GAR 25/70 3(8)

Axes are graduated in bases x 10



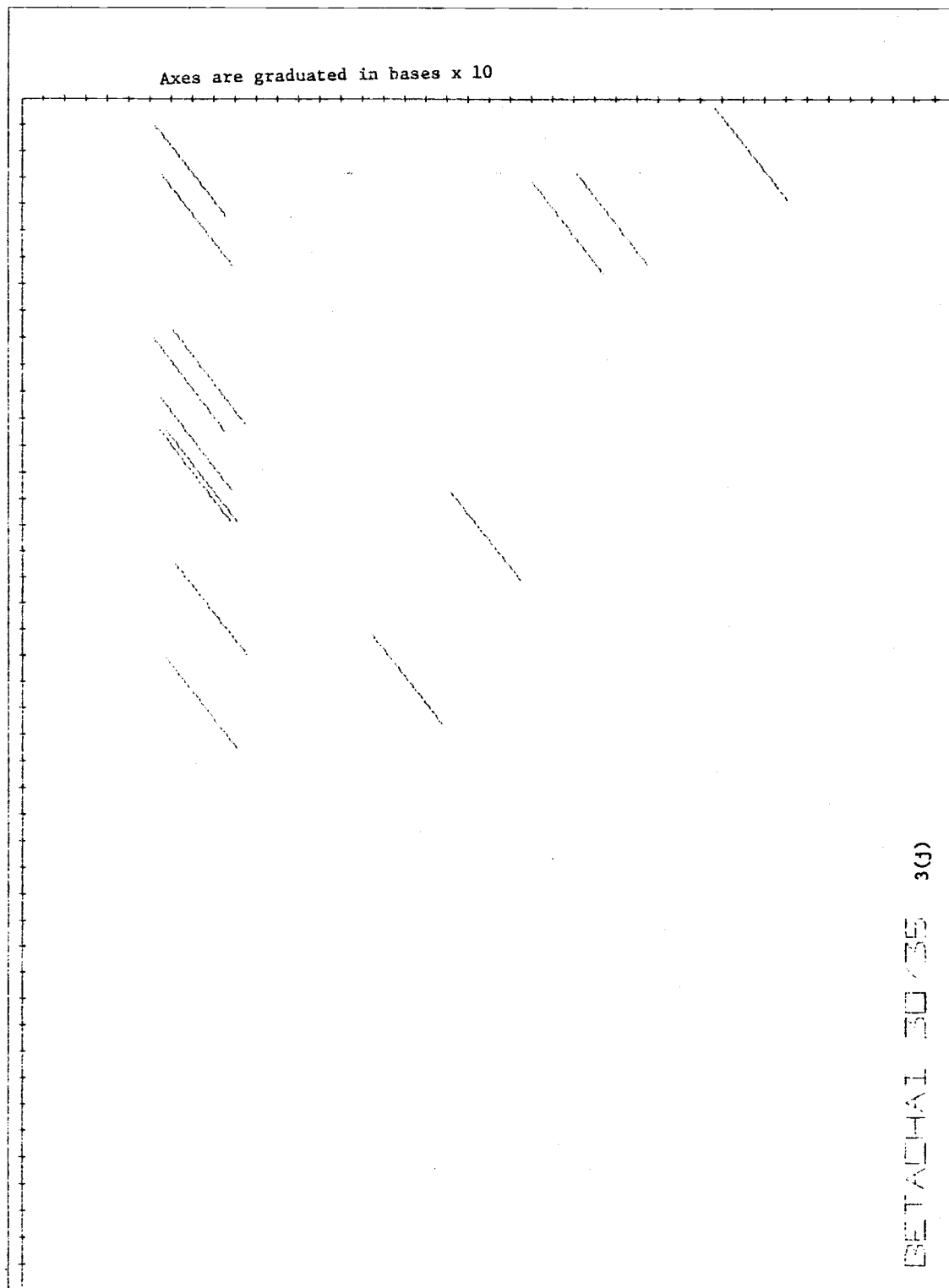
ALPHA 30/35 300

Axes are graduated in bases x 10



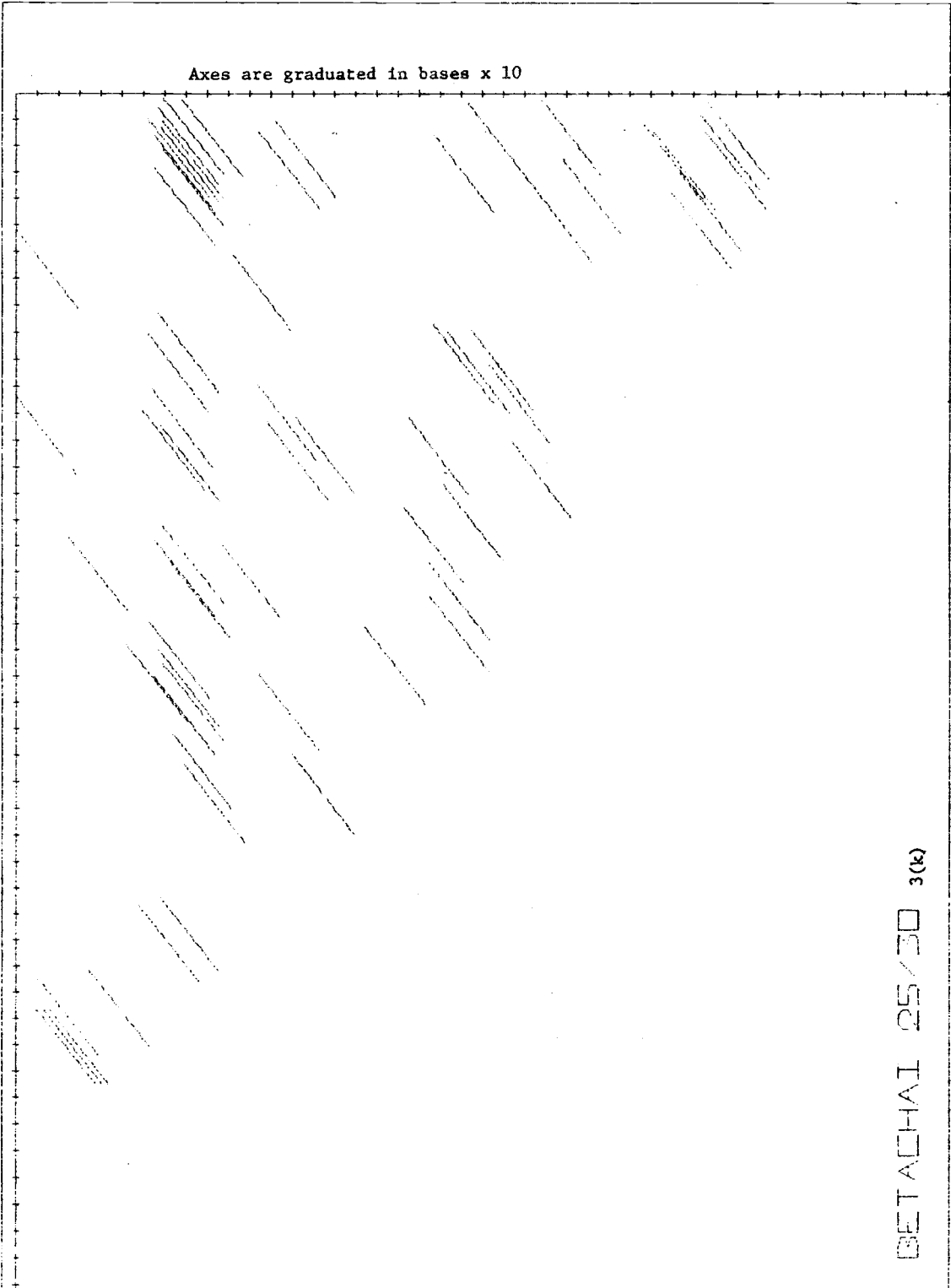
ALPHA CHA 25/30 3(4)

Axes are graduated in bases x 10



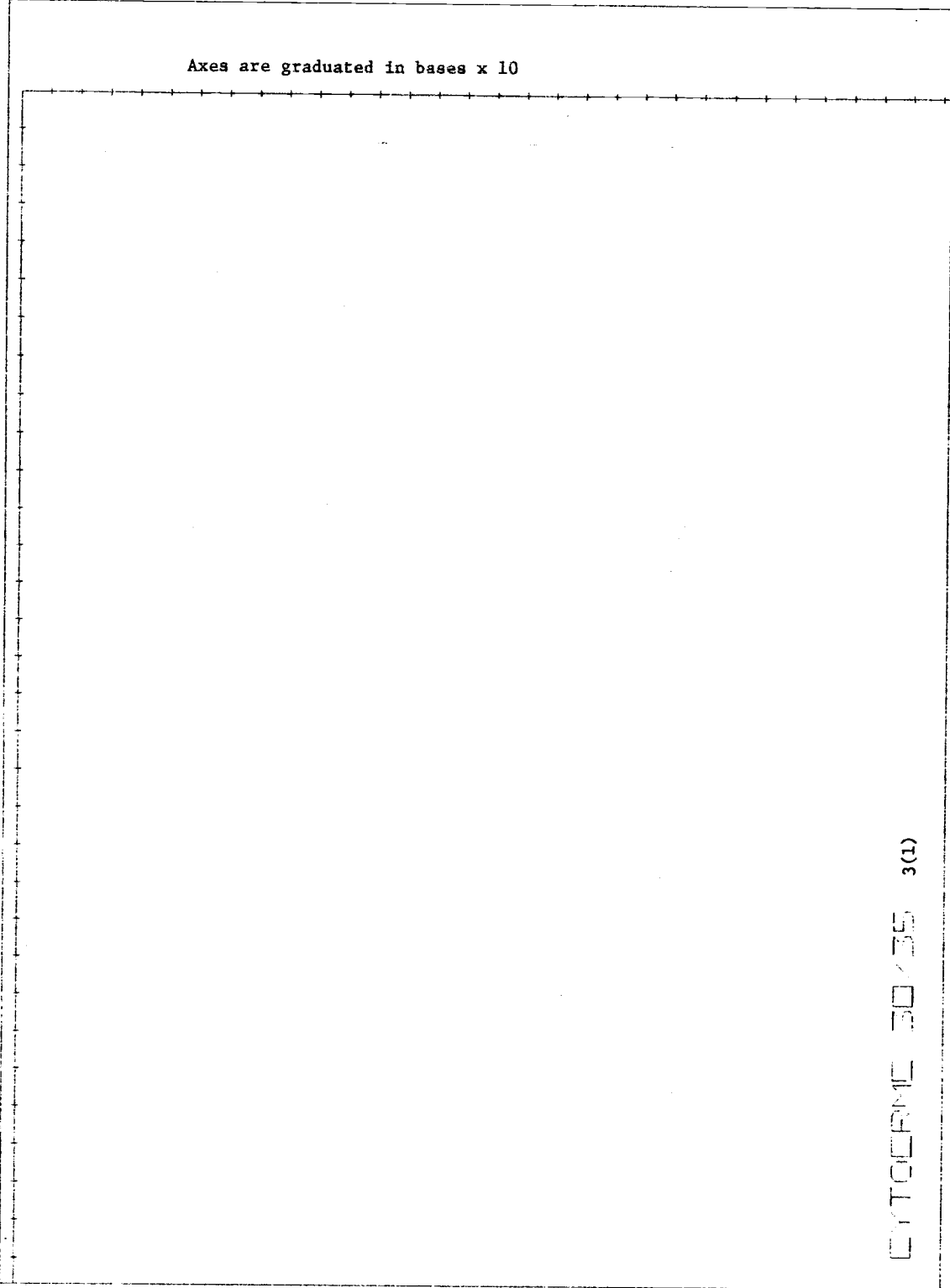
BETACHAI 30/35 30)

Axes are graduated in bases x 10



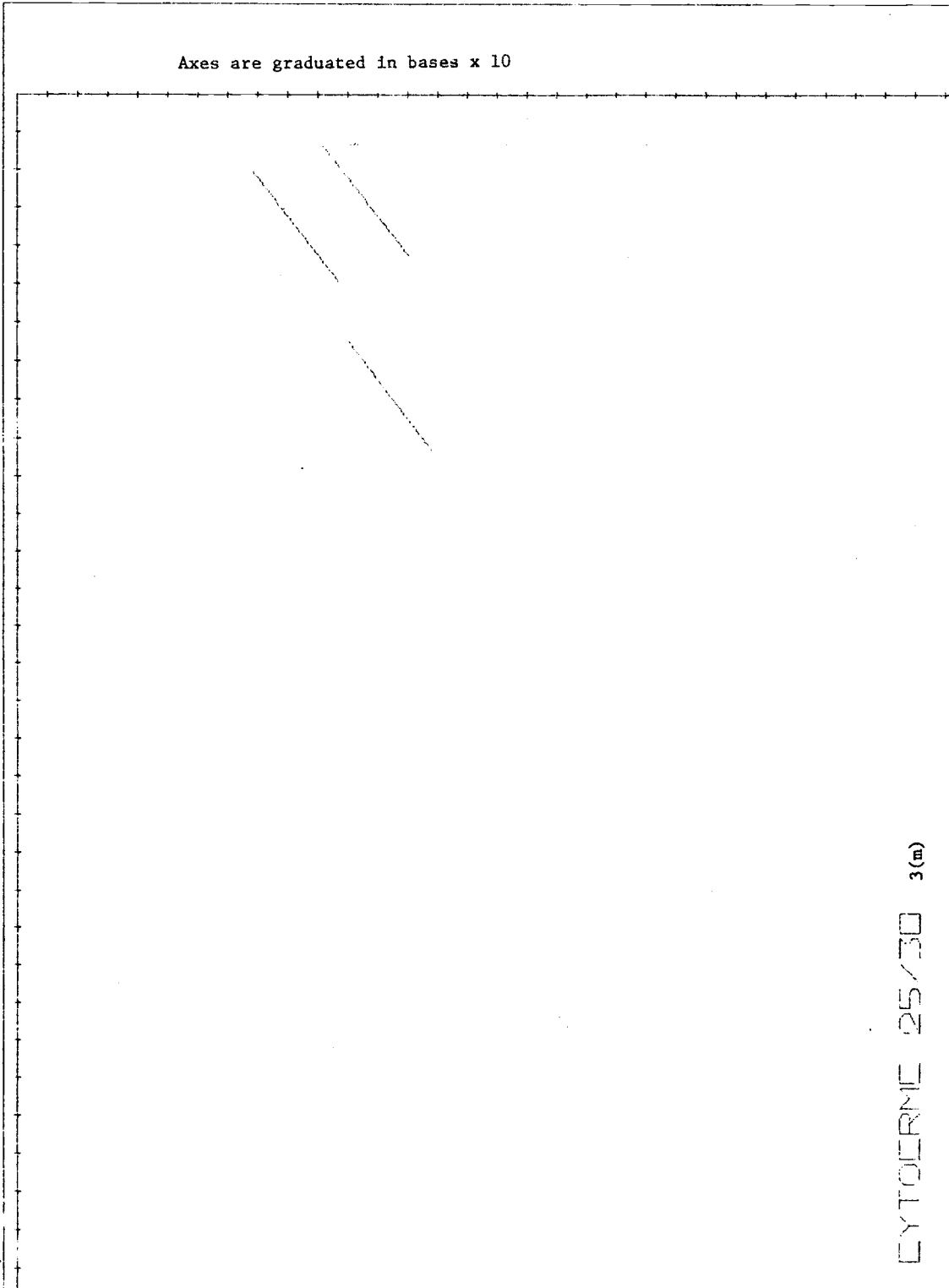
BETACHAI 25/30 3 (k)

Axes are graduated in bases x 10



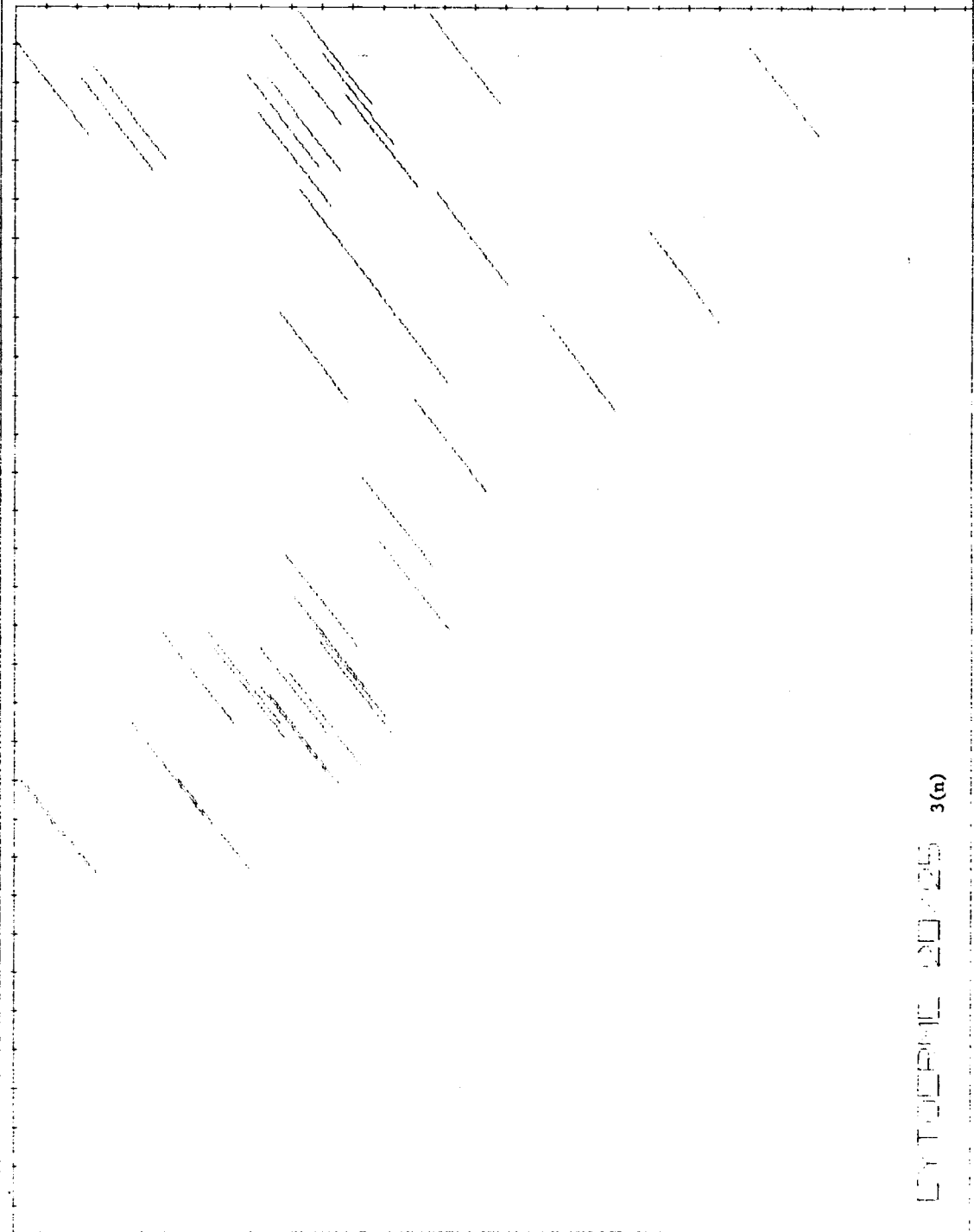
CYTOSOLIC 50/35 3(1)

Axes are graduated in bases x 10



CYTOERME 25/30 3(m)

Axes are graduated in bases x 10



CYTODERMIC 20/25 3(n)

from the test set, with the computer held at constant conditions of temperature and pressure. Here the expected hairpin loop size is nine to twelve base pairs, and, in consequence, window sizes of sixteen to eighteen were chosen. This choice stands in sharp contrast to the previous computation in which the window size used was only one tenth of the expected loop size. At the thresholds shown, the trace patterns in figure 3 emerge; the base-paired 'petals' are readily apparent.

In passing, a technique was devised to winnow the set M to some proper subset M' by taking advantage of evolutionary data. In the case of cytochrome c, for example, sequence data for 34 species, from neurospora to human, are available (38). At a given amino acid position in the protein, there are in general only a small number of residues that occur; this number ranges between one and nine for the 34 species used. The assumption was made that amino acid substitutions in cytochrome c are the result of a single point mutation. Following this assumption, a program was written to examine all possible permutations of the amino acids at any position, and to discard all arrangements in which adjacent amino acids differed by more than one base in their respective codons.

After discarding all arrangements failing the assumption, three cases were found:

- 1) no arrangements remained - this could happen if an evolutionary precursor was not included in the 34 species.
- 2) multiple arrangements remained - in this case,

phylogenetic considerations were applied to choose a likely arrangement.

- 3) a unique arrangement remained - in this case, phylogenetic considerations were still needed to validate likelihood.

In cases two and three, there were instances where a unique evolutionary path was discovered that was both consistent with the assumption and seemed to make phylogenetic sense.

The codons for each amino acid along the discovered path were then examined, and it was often possible to eliminate codons that would have contradicted the assumption. Following this strategy, one can finally end up with a proper subset of codons for the amino acid used in human cytochrome c, and by applying the algorithm at every position, a winnowing of the whole set M is achieved. The process is shown schematically in Table 3.

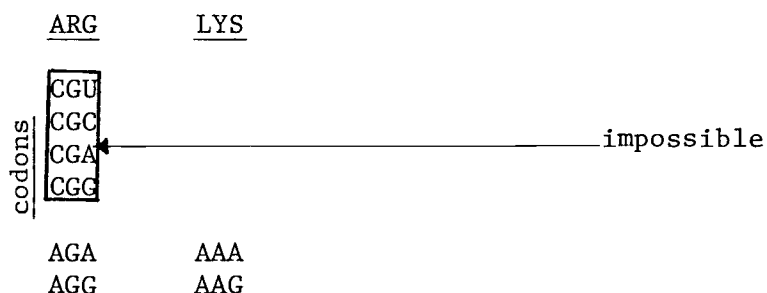
Clearly, the reliability of this method depends upon a knowledge of the true evolutionary path taken. To this extent, the final result represents only an informed guess.

Substitution of the winnowed set, M' , for the whole set M does modify the extrema \bar{m} and \underline{m} . In practical terms, though, the use of modified extrema in the experiments previously described did not change or enhance their outcome. This is not to say, however, that other experiments will not be rendered possible by the use of this technique.

In summary, the method of characteristic extrema was used to examine the genes of a representative set of proteins for the

Table 3.Winnowing of the Codon Set

At amino acid position 13 in cytochrome c, only two amino acids are used: lysine in mammals, other vertebrates, and in higher plants; and arginine in lower plants and insects. If LYS was substituted for ARG by a single point mutation, then the first four codons in the left hand column become logically impossible.

Multiple Paths

At amino acid position 39, three amino acids are used: lysine in mammals, other vertebrates, and insects; glutamine in higher plants; and histidine in two of the lower plants. Two arrangements are possible, each satisfying the assumption of a single point mutation.

Table 3 (continued)1) LYS → GLN → HIS

codons	AAA	CAA	CAU
	AAG	CAG	CAC

2) HIS → GLN → LYS

codons	CAU	CAA	AAA
	CAC	CAG	AAG

Arrangement two is the preferred one based on phylogenetic criteria.

existence of very large palindromes. The non-existence of such palindromes in the set under test prompts a conclusion that long palindromic configurations do not occur in structural genes. The possibility that a structural gene participates as a fractional part of an even larger palindrome could not be excluded by the method used.

References

1. Brown, J. E. and Klee, W. A. (1971) *Biochemistry* 10, 470-6.
2. Villarejo, M.R. and Zabin, I. (1973) *Nature New Biol.* 242,50-2.
3. Anfinsen, C.B. (1973) *Science* 181, 223-30.
4. Saxena, V.P. and Wetlaufer, D.B. (1970) *Biochemistry* 9,5015-23.
5. Baldwin, R.L. (1975) *Ann. Rev. of Biochemistry* 44, 453-475.
6. Ptitsyn, O.B., Lim, V.I., and Finkelstein, A.V. (1972) *Federation of European Biochemical Societies* 25, 421-431.
7. Levinthal, C. (1968) *J. Chim. Phys.* 65, 44-45.
8. Kuntz, I.D. (1972) *J. Am. Chem. Soc.* 94, 4009-12.
9. Lewis, P.N., Momany, F.A., Scheraga, H.A. (1971) *Proc. Nat. Acad. Sci., U.S.A.* 65, 2293-97.
10. Wetlaufer, D.B. and Ristow, S. (1973) *Ann. Rev. of Biochemistry* 42, 135-158.
11. Schulz, G.E., Barry, C.D., Friedman, J., Chou, P.Y., Fasman, G.D., Finkelstein, A.V., Lim, V.I., Ptitsyn, O.B., Kabat, E.A., Wu, T.T., Levitt, M., Robson, B., and Nagano, K. (1974) *Nature* 250, 140-42.
12. Ptitsyn, O.B. (1975) *Biophys. Chem.* 3, 1.
13. Lim, V.I. (1974) *J. Mol. Biol.* 88, 857-894.
14. Gelin, B.R. and Karplus, M. (1975) *Proc. Nat. Acad. Sci., U.S.A.* 72, 2002-2006.
15. Warme, P.K. and Scheraga, H.A. (1974) *Biochemistry* 13, 757-82.
16. Levitt, M. and Warshel, A. (1975) *Nature* 253, 694-98.
17. Marsh, R.E. and Donohue, J. (1967) *Adv. Prot. Chem.* 22, 235-56.
18. Ramachandran, G.N. and Sasisekharan, V. (1968) *Adv. Prot. Chem.* 23, 326-438.
19. Brant, D.A. and Flory, P.J. (1965) *J. Am. Chem. Soc.* 87, 2791-2800.

20. Levitt, M. (1974) *J. Mol. Biol.* 82, 393-420.
21. Ramachandran, G.N. (1972) *Conformation of Biological Molecules and Polymers; The Jerusalem Symposium on Quantum Chemistry and Biochemistry* 5, 1.
22. Szent-Gyorgyi, A.G. and Cohen, C. (1957) *Science* 126, 697.
23. Karle, I.L. and Karle, J. (1964) *Acta. Cryst.* 17, 835-41.
24. Wright, D.A. and Marsh, R.E. (1962) *Acta. Cryst.* 15, 54-64.
25. Ramachandran, G.N., Mazumdan, S.K., Venkatesan, K., and Lakshminarayanan, A.V. (1966) *J. Mol. Biol.* 15, 232-42.
26. Arnott, S. and Dover, S.D. (1967) *J. Mol. Biol.* 30, 209-12.
27. Kafatos, F.C. (1972) *Proceedings of the Vth Karolinska Symposium*, Appendix C.
28. Brawerman, G. (1974) *Ann. Rev. of Biochemistry* 43, 621-42.
29. Hirs, C.H.W., Moore, S., Stein, W.H. (1952) *J. Biol. Chem.* 200, 493-506.
30. Gilbert, W., Maizels, N., and Maxam, A. (1973) *Cold Spring Harbor Symposium* 38.
31. Nathans, D. and Smith, H.O. (1975) *Ann. Rev. of Biochemistry* 44, 273-293.
32. Wilson, D.A. and Thomas, C.A., Jr. (1974) *J. Mol. Biol.* 84, 115-144.
33. Robbins, E., Borun, T.W. (1967) *Proc. Nat. Acad. Sci., USA* 57, 409.
34. Gilmour, R.S., Dixon, G.H. (1972) *J. Biol. Chem.* 247, 4621.
35. White, H.B., Laux, B.E. and Dennis, D. (1972) *Science* 175, 1264-1266.
36. Laux, B., Dennis, D., and White, H.B. (1973) *Biochemical and Biophysical Research Communications* 54, 894-898.
37. Mark, A.J., Petruska, J.A. (1972) *J. Mol. Biol.* 72, 609-17.
38. Dayhoff, M.O. (1972) Atlas of Protein Sequence and Structure Volume 5, National Biomedical Research Foundation, Wash. D.C.

39. Tinoco, I., Jr., Uhlenbeck, O.C. and Levine, M.D. (1971)
Nature 230, 362-367.
40. Brezinski, D.P. (1975) Nature 253, 128-130.

APPENDIX

PROTEINS LIBRARY

PROGRAM AALIST

```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C PROGRAM TO LIST THE AMINO ACID SEQUENCE
C FROM A PROTEIN
C PARAMETERS ARE THE PROTEIN FILE NAME AND
C THE NUMBER OF THREE LETTER CODES PER LINE
C
C OUTPUT DIRECTED TO LUN 12
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C

```

PROGRAM ADDHV2

```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C PROGRAM TO READ A CRYSTALLOGRAPHIC STRUCTURE AND
C AUGMENT IT BY ADDING H ATOMS TO THE MAIN CHAIN AND TO
C THE SIDE CHAINS OF THE FOLLOWING RESIDUES
C SER,THR,TYR,LYS,ARG
C
C OUTPUT TO LUN 12
C OUTPUT AUGMENTED FILE TO LUN 13
C
C WORKS WITH FILE OF COORDINATES*10.
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```

PROGRAM BENDER

```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C PROGRAM TO COMPUTE SUCCESSIVE DIHEDRAL AND BEND ANGLES
C FOR THE BYRON BENDER
C INPUT IS THE ATOMIC COORDINATES FOR A PROTEIN
C

```

```
C  OUTPUT TO LUN 12, WHICH IS                               C
C  EQUIPPED AS A FILE IF NOT ALREADY EQUIPPED             C
C  REWOUND IF A FILE                                       C
C                                                           C
C  CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
```

```
PROGRAM CONMAP
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C  PROGRAM TO PRINT OUT THE 10A CONTACT MAP                 C
C  FROM THE COORDINATES FOR A PROTEIN                     C
C                                                           C
C  CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
```

```
PROGRAM DIHEDRAL
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C  PROGRAM TO PRINT OUT THE PHI,PSY,AND CHI DIHEDRAL ANGLES C
C  FOR A PROTEIN WITH KNOWN COORDINATES                   C
C                                                           C
C  OUTPUT DIRECTED TO LUN 12                               C
C  OUTPUT CONSISTS OF COORDINATE DATA                    C
C  THEN A FILE MARK                                        C
C  THEN DIHEDRAL ANGLES                                    C
C  FOLLOWED BY A SECOND FILE MARK                          C
C                                                           C
C  CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
```

```
PROGRAM EPATH
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C  PROGRAM TO FIND AN EVOLUTIONARY PATH THROUGH AN AMINO ACID C
C  SEQUENCE.                                               C
C  CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C  SUBROUTINE ALLPATHS(N,JAA,JNUM,JPATHS)
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C  SUBROUTINE TO FIND ALL POSSIBLE EVOLUTIONARY PATHS WITH C
C  DISTANCE 1 THROUGH N AMINO ACIDS                       C
C  EACH POSSIBLE PATH IS CHARACTERIZED BY ITS             C
C  PERMUTATION NUMBER.                                     C
C  OUTPUT IS RETURNED IN JPATHS. IT CONSISTS OF JNUM PERMUTATION C
C  NUMBERS, ONE FOR EVERY LEGAL PATH.                     C
```

```

C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```

```

PROGRAM NEXTRFS

```

```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C PROGRAM NEXT RESIDUE
C PROGRAM TO START FROM THE N-TERMINAL END OF A PROTEIN
C AND STOPPING AT CHOSEN SPOTS, TO ADD A RESIDUE
C
C INPUT COORDINATES SHOULD BE IN ANGSTROMS*10
C
C SINCE WORKATOM COORDINATES GET SUPERIMPOSED ON THE COORD ARRAY
C IT IS NECESSARY TO WORK FROM THE C TERMINAL END BACK
C TO THE N-TERMINAL END WHEN MAKING POTENTIAL MAPS
C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```

```

PROGRAM PDISPLAY

```

```

CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C PROGRAM TO DISPLAY A POLYPEPTIDE
C OPTIONS INCLUDE
C DISPLAY WITH ALPHA CARBONS INDEXED
C WHOLE BACKBONE SELECTIVELY DISPLAYED
C SIDE GROUPS SELECTIVELY DISPLAYED
C INDIVIDUAL ACID TYPES MAY BE SELECTIVELY DISPLAYED
C PARTICULAR RANGES MAY BE SELECTIVELY DISPLAYED
C
C H-HARD COPY
C SP-ROTATE THE PICTURE
C R-RESET
C DEL-EXIT
C Z-ZOOM
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
SUBROUTINE LABEL(JJ, JRDT, KOPY)
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C SUBROUTINE TO LABEL THE ALPHA CARBONS.
C PARAMETERS ARE-
C JJ= ALPHA CARBON SEQUENCE NUMBER
C JRDT= 0 IF LEFT FIGURE, 4 IF RIGHT FIGURE
C
C LABEL DESTROYS THE CURRENT SCALING AND ROTATION
C

```

```

C
C

```

```

PROGRAM PLANECK

```

```

C
C
C PROGRAM TO CHECK THE BACKBONE PLANARITY OF A POLYPEPTIDE CHAIN.
C TAKES THE PLANES CA-N-H AND
C CA-C O
C AND ESTABLISHES A NORMAL TO EACH PLANE. THEN MEASURES THE ANGLE
C BETWEEN THE TWO NORMALS.
C
C ALL OUTPUT IS DIRECTED TO LUN 12 WHICH IS EQUIPPED TO RE A FILE
C UNLESS OTHERWISE EQUIPPED
C
C
C

```

```

PROGRAM POLYMER

```

```

C
C
C PROGRAM TO PRODUCE A POLYMER WITH SPECIFIED
C PRIMARY STRUCTURE
C ALL TORSTON ANGLES IN BACKBONE ARE 180
C WLL SIDE CHAIN ANGLES ARE 0
C INPUT FROM A NAMED FILE
C OUTPUT TO LUN 12
C
C
C

```

```

PROGRAM SHUFFLE

```

```

C
C
C PROGRAM TO CANGE THE ORDER OF A FILE OF ATOMIC COORDINATES
C FROM THE ORDER N,H,CA,HA,CB,...,C,O
C TO THE ORDER CA,N,H,C,O,HA,CB,...
C
C INPUT FROM A NAMED FILE
C OUTPUT TO LUN 12
C
C
C

```

```

      PROGRAM SYNTHESIZE
      CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
      C
      C SYNTHESIZE A BACKBONE THAT IS NUMRES LONG.
      C READS NUMRES (PHI,PSY) ANGLES FROM A FILE AND
      C TWISTS THE BACKBONE ACCORDING TO THE INTOWELL TRANSFORM
      C OF THOSE SPECIFIED ANGLES
      C PRO AND GLY ARE NOT TRANSFORMED, HOWEVER.
      C
      CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
      C SUBROUTINE INTOWELL(A1,A2,A3,A4)
      CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
      C
      C SUBROUTINE TO COMPUTE THE DIHEDRAL ANGLES OF AN ENERGY WELL
      C THAT IS CLOSEST TO THE RAMACHANDRAN POSITION SPECIFIED
      C BY A DIHEDRAL ANGLE PAIR (A1,A2)
      C
      C A1,A2 ARE THE ACTUAL (PHI,PSY) ANGLES
      C A3,A4 ARE DIHEDRAL ANGLES OF THE CLOSEST WELL
      C
      C ALL ANGLES ARE IN DEGREES
      C
      CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```

```

      PROGRAM TRUER
      CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
      C
      C PROGRAM TO COMPUTE A BASE PLANE AND MARK SELECTED
      C RESIDUES FOR "TUNING-UP" A RENDER MODEL.
      C
      C INPUT CONSISTS OF
      C 1) ATOMIC COORDINATES FOR THE PROTEIN
      C 2) A FILE OF RESIDUES OF INTEREST. THE FIRST THREE OF
      C THESE RESIDUES ARE TAKEN TO DEFINE THE ZERO PLANE
      C FILE SHOULD CONTAIN ONE RESIDUE PER RECORD
      C
      C KEY RESIDUES 1 AND 2 ARE LINED UP ALONG THE + X-AXIS
      C IN THIS ORIENTATION, THE PROGRAM ASKS WHETHER KEY RESIDUE
      C 3 HAS POSITIVE OR NEGATIVE Y COORDINATE (IN THE XY PLANE
      C THIS INFORMATION IS USED TO ROTATE THE COORDINATES
      C INTO STANDARD ORIENTATION
      C
      C OUTPUT CONSISTS OF COORDINATES OF THE BENCH MARK RESIDUES
      C TOGETHER WITH A SCALED PLOT OF THEIR (X,Y) POSITIONS
      C

```


C
 CCC

PROGRAM UNHEND

CC
 C
 C PROGRAM TO COMPUTE A SET OF CONSISTENT C ALPHA COORDINATES C
 C FROM THE DIHEDRAL AND BEND ANGLES C
 C
 C INPUT IS A FILE CONSISTING OF RECORDS, EACH CONTAINING C
 C DIHEDRAL ANGLE...BEND ANGLE...CA(I)-CA(I+1) LENGTH C
 C
 C OUTPUT TO LUN 12, WHICH IS C
 C EQUIPPED AS A FILE IF NOT ALREADY EQUIPPED C
 C REWIND IF A FILE C
 C
 CCC

PROGRAM OLIGOPEP

CC
 C
 C PROGRAM TO COMPUTE OLIGOPEPTIDE ENERGIES C
 C
 C INPUT CONSISTS OF C
 C 1) SOME FILES OF (PHI,PSY) PAIRS WHICH COMPRISE THE DOMAINS C
 C FOR THE BACKBONE ANGLES SETS C
 C 2) SOME FILES OF SIDE CHAIN ANGLES THAT COMPRISE THE C
 C DOMAINS OF SIDE CHAIN ANGLE SETS C
 C 3) A FILE THAT MAPS EACH RESIDUE INTO ONE AND ONLY ONE C
 C OF THE DOMAIN SETS. CONSISTS OF A DOMAIN NUMBER C
 C PER RECORD AND ASSUMED TO BE IN RESIDUE ORDER C
 C 4) A FILE THAT MAPS EACH SIDECHAINS BONDS INTO ITS DOMAIN C
 C OF DEFINITION. THE FILE HAS ONE RECORD FOR EACH RESIDUE C
 C EVERY SUCH RECORD HAS K ITEMS, ONE FOR EACH ROTATABLE C
 C BOND IN THE SIDE CHAIN OF THAT RESIDUE C
 C 5) A FILE OF COORDINATES FOR THE OLIGOPEPTIDE AS IT C
 C EXISTS IN TOTALLY UNFOLDED CONFORMATION, I.E. C
 C WITH BACKBONE ANGLES=180 AND SIDECHAIN ANGLES=0 C
 C
 C OUTPUT CONSISTS OF C
 C 1) A FILE NAMED WHY OF ALLOWED CONFIGURATIONS C
 C 2) A FILE NAMED WHYNOT OF CONTACT INHIBITED CONFIGURATIONS C
 C

CC

RNA LIBRARY

PROGRAM AATDAIL

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CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C   PROGRAM TO READ A FILE OF AMINO ACIDS AND TRANSLATE      C
C   THEM TO AUGONS                                           C
C   OUTPUT TO LUN 12                                         C
C   INPUT HAS ONE AMINO ACID PER RECORD=3 LETTER CODES     C
C   OUTPUT HAS UP TO 2 AUGONS PER RECORD                     C
C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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PROGRAM EPATH

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CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C   PROGRAM TO FIND THE EVOLUTIONARY PATHS THROUGH           C
C   A SERIES OF AMINO ACIDS.                                 C
C   INPUT IS AN AMINO ACID SEQUENCE WITH EVOLUTIONARY      C
C   ALTERNATIVES. EACH RECORDS IS OF THE FORM              C
C   ITH AA  AA1,AA2,...,AAJ                                 C
C   OUTPUT IS A SERIES OF AUGONS WHERE EACH RECORD IS      C
C   OF THE FORM                                             C
C   ITH AA  AUG1,AUG2                                       C
C
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PROGRAM FDLDRNA

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CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C   PROGRAM TO INSPECT AN AUGON CHAIN, IDENTIFY             C

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SUBROUTINE CODONIDX(CNAME,INDXACID)
SUBROUTINE TO TRANSLATE A 3 CHARACTER CODON NAME
INTO THE INDEX NUMBER OF THE AMINO ACID IT CODES FOR.
STOP IS CODED AS A 0 INDEX.
PARAMETERS ARE-

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    CNAME= A 3 CHARACTER RCD NAME
    INDXACID= THE INDEX NUMBER
THE ROUTINE READS THE CNAME PARAMETER AND
PLACES THE APPROPRIATE INDEX NUMBER INTO
INDXACID.
THE ROUTINE COMES TO AN ERROR HALT IF AN ILLEGAL
CODON IS ENCOUNTERED.

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PROGRAM CONTACT
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
FUNCTION CONTACT
DISTANCE=CONTACT(JATOM1,JATOM2)
GIVES MINIMUM CONTACT DISTANCES IN ANGSTROMS FOR ANY
TWO OF THE FOLLOWING SET
H,D,N,C, AND CH=METHYL GROUP

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ATOM NAMES SHOULD BE LEFT JUSTIFIED
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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PROGRAM COVRADII
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
SUBROUTINE COVRADII(IDXATOM,DIST)
SUBROUTINE TO DETERMINE THE COVALENT RADIUS
FOR AN ATOM
PARAMETERS ARE-
    IDXATOM = THE ATOMIC SYMBOL INDEX NUMBER
    DIST = THE COVALENT RADIUS IN ANGSTROMS
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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PROGRAM DISTANCE
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
SUBROUTINE DISTANCE(JCODON1,JCODON2,MEASURE)
SUBROUTINE TO MEASURE THE EVOLUTIONARY DISTANCE
BETWEEN 2 ARBITRARY CODONS. MEASURES THE NUMBER
OF BASE CHANGES BETWEEN THE TWO. SO THE FUNCTION
YIELDS A VALUE BETWEEN 0 AND 3.

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SUBROUTINE IDXATLAS(INDXACID,NAMFACID)
SUBROUTINE TO TRANSLATE AN INDEX NUMBER [1-20]
TO A 1 CHARACTER AMINO ACID NAME.
PARAMETERS ARE-
  INDXACID= THE INDEX NUMBER
  NAMEACID= A 1 CHARACTER HCD NAME
THE ROUTINE READS THE INDXACID PARAMETER AND
PLACES THE APPROPRIATE NAME INTO
NAMEACID.
THE ROUTINE COMES TO AN ERROR HALT IF AN ILLEGAL
INDEX NUMBER IS ENCOUNTERED.
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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PROGRAM      IDXATOM
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
SUBROUTINE IDXATOM(INDEX,NAMEATOM)
SUBROUTINE TO TRANSLATE AN INDEX NUMBER TO
AN ATOMIC SYMBOL.
PARAMETERS ARE -
  INDEX - AN ATOM INDEX
  NAMEATOM - AN ATOMIC SYMBOL
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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PROGRAM      IDXAUGDN
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
SUBROUTINE IDXAUGDN(INDEX,NUM,JARRAY)
SUBROUTINE TO TRANSLATE AN ALPHABETIC AMINO ACID INDEX
NUMBER INTO A LIST OF COLLAPSED CODONS THAT CODE FOR
THAT ACID.
INDEX NUMBER 0 IS THE STOP CODE

COLLAPSED CODONS INCLUDE A,C,G,U, AND
M=MASTER=(U,A,G,C)
Y=PYRIMIDINE=(U,C)
R=PURINE=(A,G)

PARAMETERS ARE-
  IDX - AN ALPHABETIC INDEX NUMBER
  NUM - THE NUMBER OF CODONS THAT CODE FOR THE A.A.
  JARRAY - AN ARRAY POINTER WHERE THE 3 CHARACTER CODES
          OF THE CODONS WILL BE PLACED, 1 CODON/WORD,
          LEFT JUSTIFIED

```

THE ROUTINE READS THE INDEX AND PLACES THE APPROPRIATE NUMBER OF CODONS INTO NUM. THEN THE 3 CHARACTER CODON CODES ARE PLACED INTO EACH SUCCESSIVE ELEMENT OF JARRAY.

THE ROUTINE COMES TO AN ERROR HALT IF AN ILLEGAL INDEX NUMBER IS ENCOUNTERED.

CC

PROGRAM IDXCODON

CC

SUBROUTINE IDXCODON(INDEX,NUM,JARRAY)

SUBROUTINE TO TRANSLATE AN ALPHABETIC AMINO ACID INDEX NUMBER [0-20] INTO A LIST OF CODONS THAT CODE FOR THAT ACID. INDEX NUMBER 0 IS THE STOP CODE.

PARAMETERS ARE-

IDX= AN ALPHABETIC INDEX NUMBER

NUM= THE NUMBER OF CODONS THAT CODE FOR THE AMINO ACID

JARRAY= AN ARRAY POINTER WHERE THE 3 CHARACTER CODES OF TH CODONS WILL BE PLACED, 1 CODON/WORD, LEFT JUSTIFIED

THE ROUTINE READS THE INDEX AND PLACES THE APPROPRIATE

NUMBER OF CODONS INTO NUM. THEN THE 3 CHARACTER CODON CODES ARE PLACED INTO EACH SUCCESSIVE ELEMENT OF JARRAY.

THE ROUTINE COMES TO AN ERROR HALT IF AN ILLEGAL INDEX NUMBER IS ENCOUNTERED.

CC

PROGRAM INVCODON

CC

SUBROUTINE INVCODON(J1,J2)

PARAMETERS ARE-

J1 = A LEFT JUSTIFIED COD 3 CHARACTER CODON

J2 = ANTCODON FOR J1

CC

SUBROUTINE JEFFREYS(A,B,POINT,THETA)

CC

C

C OPERATOR TO ROTATE A POINT(X,Y,Z) BY THETA DEGREES
C ABOUT A LINE FROM A TO B

C

C A IS CONSTRUED TO BE THE ORIGIN

C B IS A POINT ON THE AXIS LINE THROUGH THE ORIGIN

SUBROUTINE TO FIND ALL POSSIBLE PERMUTATIONS OF N OBJECTS
PARAMETERS ARE

N - THE NUMBER OF OBJECTS. IF N=0, PERMUTE DELIVERS
THE NEXT PERMUTATION OVER THE LAST NON-ZERO N.
NEXTPERM= THE NEXT PERMUTATION OF N OBJECTS, EXPRESSED AS
A BASE N NUMBER. IF ALL PERMUTATIONS HAVE BEEN
EXHAUSTED, NEXTPERM=0

LIMITATION= N CANNOT EXCEED 9 BECAUSE OF THE WAY NEXTPERM
IS EXPRESSED (I.E. AS A DIGIT). OF COURSE
IN PRACTICE, NEXTPERM CANNOT EXCEED 2²⁴-1

CC

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PROGRAM      REVCODON
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
SUBROUTINE REVCODON(J1,J2)
PARAMETERS ARE-
  J1 - A LEFT JUSTIFIED BCD 3 CHARACTER CODON
  J2 - REVERSE CODON FOR J1
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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PROGRAM      ASTRING,JSTRING,DSTRING
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
FUNCTION ASTRING(BUFF,JSTART,LNGBUFF)
  OR
FUNCTION DSTRING(BUFF,JSTART,LNGBUFF)

```

FUNCTION TO SCAN OFF AN ALPHANUMERIC SYMBOL OR A NUMBER
AND RETURN THE RESULTS IN AQ.

PARAMETERS ARE-
BUFF=THE FWA OF THE BUFFER IN WHICH THE STRING IS FOUND
JSTART=A CHARACTER POSITION POINTER ON THAT BUFFER
LNGBUFF=CHARACTER LENGTH OF THE BUFFER

UPON EXIT, THE SCANNED ITEM WILL BE IN AQ, AND JSTART WILL BE
UPDATED TO THE LAST CHARACTER SCANNED+1

THIS ROUTINE WILL NOT SCAN BEYOND LNGBUFF. BLANKS AND SPECIAL
CHARACTERS ARE IGNORED. AN ALPHA STRING IS TERMINATED
AFTER 8 CHARACTERS ARE ACCRUED OR WHEN A NON-ALPHANUMERIC
IS ENCOUNTERED.


```

C
C   SUBROUTINE TO FIND THE ANGLES (THETA,PHI)
C   NECESSARY TO ROTATE AN ARBITRARY VECTOR, VEC,
C   SO THAT IT IS PARALLEL TO THE X-AXIS AND POINTING
C   IN THE POSITIVE DIRECTION
C   THETA = DISPLACEMENT FROM THE YZ PLANE
C           WHEN ROTATING AROUND X AXIS
C   PHI   = DISPLACEMENT FROM THE X AXIS
C           WITHIN THE XZ PLANE
C           WHEN ROTATING AROUND Y AXIS
C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```

```

      SUBROUTINE ROTXY(THETA,V)
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C   SUBROUTINE TO PERFORM A ROTATION IN THE XY PLANE
C   ROTATION WILL BE IN THE CLOCKWISE DIRECTION VIEWED
C   FROM THE (+) Z-AXIS
C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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```

      SUBROUTINE ROTYZ(THETA,V)
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C   SUBROUTINE TO PERFORM A ROTATION IN THE YZ PLANE
C   ROTATION WILL BE IN THE CLOCKWISE DIRECTION
C   VIEWED FROM THE (+) X-AXIS
C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

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```

      SUBROUTINE ROTXZ(THETA,V)
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC
C
C   SUBROUTINE TO PERFORM A ROTATION IN THE XZ PLANE
C   ROTATION WILL BE IN THE CLOCKWISE DIRECTION
C   VIEWED FROM THE (+) Y-AXIS
C
CCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCCC

```

PROGRAM VDWPRATI

